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### Centro de Tecnologia e Ciências Instituto de Química

Milena Mendonça Guimarães

Study of the catalytic conversion of CO<sub>2</sub> to CO by Reverse Water-Gas Shift Reaction (RWGS) as a decarbonization alternative for the petroleum industry

> Rio de Janeiro 2024

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Dissertação apresentada, como requisito parcial para obtenção do título de Mestre, ao Programa de Pós-Graduação em Engenharia Química, da Universidade do Estado do Rio de Janeiro.

Área de concentração: Processos Químicos, Petróleo e Meio-ambiente.

Orientadores: Prof.<sup>a</sup> Dr<sup>a</sup>. Fatima Maria Zanon Zotin

Prof. Dr. André Luiz Hemerly Costa

Prof.<sup>a</sup> Dr<sup>a</sup>. Lucia Gorenstin Appel

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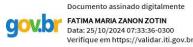
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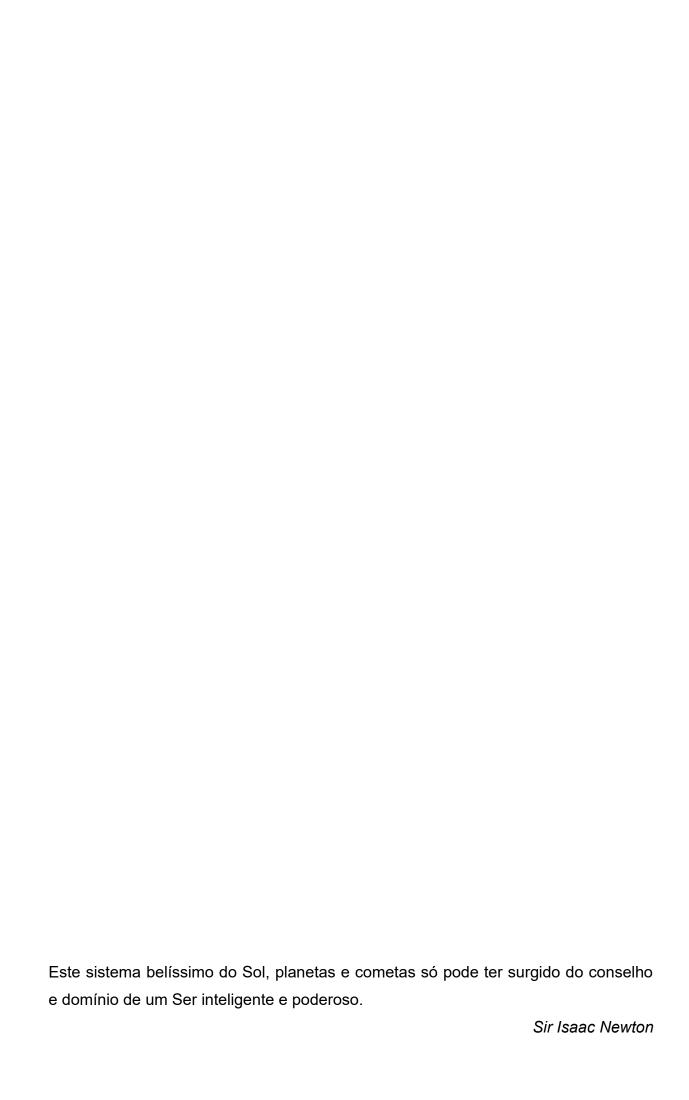
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### **RESUMO**

GUIMARÃES, M. M. Study of the catalytic conversion of CO<sub>2</sub> to CO by Reverse Water-Gas Shift Reaction (RWGS) as a decarbonization alternative for the petroleum industry. 2024. 111 f. Dissertação (Mestrado em Engenharia Química) – Instituto de Química, Universidade do Estado do Rio de Janeiro, Rio de Janeiro, 2024.

O aumento contínuo da concentração de gases do efeito estufa na atmosfera desde a Revolução Industrial é a origem das mudanças climáticas que acometem o planeta. A resolução dessa questão passa pela redução das emissões antropogênicas de CO<sub>2</sub>; desta forma, torna-se importante desenvolver alternativas para aproveitar o CO<sub>2</sub> como matéria-prima para a obtenção de produtos de interesse comercial. A reação de deslocamento gás-água reversa (bastante conhecida pelo seu nome em inglês, reverse water-gas shift, comumente abreviado como RWGS), apontada como uma rota promissora nos esforços direcionados à descarbonização, consiste na hidrogenação do dióxido de carbono, dando origem a água e monóxido de carbono, que, por sua vez, é amplamente empregado na indústria química para a fabricação de uma grande variedade de produtos. No entanto, a existência de reações competitivas e a natureza endotérmica da reação RWGS fazem com que sua aplicação em escala industrial exija o desenvolvimento de catalisadores mais ativos e seletivos, processo que necessariamente envolve a busca por um conhecimento mais profundo da cinética da reação. Nesse contexto, o presente trabalho tem o objetivo de estudar o desempenho do catalisador comercial de CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> sob diferentes condições operacionais e obter valores de parâmetros cinéticos para as expressões de taxa de reação disponíveis na literatura. Para esse fim, foram realizados testes em temperaturas fixas de 330 °C, 380 °C e 430 °C (testes em patamares de temperatura) sob diferentes velocidades espaciais (18 m³ kg<sup>-1</sup> h<sup>-1</sup>, 30 m³ kg<sup>-1</sup> h<sup>-1</sup> e 42 m³ kg<sup>-1</sup> h<sup>-1</sup>) e razões molares H<sub>2</sub>/CO<sub>2</sub> (1:1, 2.5:1 e 4:1), além de testes em rampa de temperatura (testes de light-off) da temperatura ambiente até 500 °C. A seletividade a monóxido de carbono obtida foi de 100% em todos os experimentos. Os testes em patamares de temperatura permitiram verificar que maiores temperaturas, maiores razões H<sub>2</sub>/CO<sub>2</sub> e menores velocidades espaciais proporcionam conversões de CO<sub>2</sub> mais altas. Os parâmetros cinéticos foram ajustados a partir dos dados experimentais das curvas de light-off fornecidas pelos testes em rampa de temperatura, devido à concordância observada entre essas curvas e os resultados dos testes isotérmicos. Os parâmetros foram estimados usando um modelo pseudo-homogêneo de reator de leito fixo em estado estacionário, aplicando as expressões de taxa de reação propostas por três diferentes grupos de pesquisa. A simulação das curvas de light-off com os parâmetros obtidos forneceu uma previsão satisfatória das tendências observadas experimentalmente, indicando que as curvas de *light-off* podem ser uma abordagem prática para a extração de informações cinéticas de uma forma mais simples e com menor número de experimentos necessários.

Palavras-chave: CO<sub>2</sub>; catálise; descarbonização; reação de deslocamento gás-água reversa; modelagem.

### **ABSTRACT**

GUIMARÃES, M. M. Study of the catalytic conversion of CO<sub>2</sub> to CO by Reverse Water-Gas Shift Reaction (RWGS) as a decarbonization alternative for the petroleum industry. 2024. 111 f. Dissertação (Mestrado em Engenharia Química – Instituto de Química, Universidade do Estado do Rio de Janeiro, Rio de Janeiro, 2024.

The continuous increase in the concentration of greenhouse gases in the atmosphere since the Industrial Revolution is the origin of the climate change that affects the planet. The solution to this issue involves reducing anthropogenic CO<sub>2</sub> emissions; therefore, it is important to develop alternatives for employing the CO<sub>2</sub> as a raw material to obtain products with commercial interest. The reverse water-gas shift reaction (commonly abbreviated as RWGS), identified as a promising route in efforts aimed at decarbonization, consists of the hydrogenation of carbon dioxide, giving rise to water and carbon monoxide, which, in turn, is widely used in the chemical industry to manufacture a broad variety of products. However, the existence of competitive reactions and the endothermic nature of the RWGS reaction mean that its application on an industrial scale requires the development of more active and selective catalysts, a process that necessarily involves the search for a deeper understanding of the reaction kinetics. In this scenario, the present work aims to study the performance of the commercial CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst under different operating conditions and to obtain kinetic parameter values for reaction rate expressions available in the literature. For this purpose, tests were performed at fixed temperatures of 330 °C, 380 °C and 430 °C (tests at temperature levels) under different space velocities (18 m³ kg<sup>-1</sup> h<sup>-1</sup>, 30 m³ kg<sup>-1</sup> h<sup>-1</sup> and 42 m³ kg<sup>-1</sup> h<sup>-1</sup>) and H<sub>2</sub>/CO<sub>2</sub> molar ratios (1:1, 2.5:1 and 4:1), in addition to temperature ramp tests (lightoff tests) from room temperature to 500 °C. The selectivity to carbon monoxide obtained was 100% in all experiments. The fixed-temperature tests allowed verifying that higher temperatures, higher H<sub>2</sub>/CO<sub>2</sub> ratios, and lower space velocities provide higher CO<sub>2</sub> conversions. The kinetic parameters were fitted from the experimental data of the light-off curves provided by the temperature ramp tests, due to the agreement observed between these curves and the results of the isothermal tests. The parameters were estimated using a pseudo-homogeneous model of a steadystate fixed-bed reactor, applying the reaction rate expressions proposed by three different research groups. The simulation of the light-off curves with the obtained parameters provided a satisfactory prediction of the experimentally observed trends, indicating that the light-off curves can be a practical approach for the extraction of kinetic information in a simpler way and with a smaller number of experiments required.

Keywords: CO<sub>2</sub>; catalysis; decarbonization; reverse water-gas shift reaction; modeling.

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### LISTA DE ABREVIATURAS E SIGLAS

CCS Carbon Capture and Storage

CCU Carbon Capture and Utilization

CCUS Carbon Capture, Utilisation and Storage

FTS Fischer-Tropsch Synthesis

GHSV Gas Hourly Space Velocity

IBP Instituto Brasileiro de Petróleo e Gás

IEA International Energy Agency

IPCC Intergovernmental Panel on Climate Change

ECMWF European Center for Medium-Range Weather Forecasts

NIST National Institute of Standards and Technology

RWGS Reverse Water-Gas Shift

WGS Water-Gas Shift

### LISTA DE SÍMBOLOS

• • •	0	
$\Delta G^{\circ}_{298  K}$	Standard Gibbs free energy of formation at 298 K (kJ mol <sup>-1</sup> )	

Standard enthalpy of reaction at 298 K (kJ mol<sup>-1</sup>) ΔH°<sub>R. 298 K</sub>

S Vacant active sites (dimensionless)

Rate of reaction j (mol g<sup>-1</sup> h<sup>-1</sup>, mol kg<sup>-1</sup> s<sup>-1</sup>) rį

Rate constant of the RWGS reaction (atm<sup>-1</sup> h<sup>-1</sup>, mol kg<sup>-1</sup> s<sup>-1</sup> bar<sup>-1</sup>, mol kg<sup>-1</sup> s<sup>-1</sup> bar<sup>-0.5</sup>)  $k_1$ 

Concentration of active sites of fresh catalyst (mol g<sup>-1</sup>)  $L_0$ 

 $P_i$ Partial pressure of component i (Pa, atm, bar)

 $K_1$ Equilibrium constant of the RWGS reaction (dimensionless)

 $K_8*$ Equilibrium constant of reaction (8) (atm<sup>-1</sup>)

 $K_{24}^{*}$ Equilibrium constant of reaction (24) (atm)

Adsorption equilibrium constant for H<sub>2</sub>O (bar<sup>-1</sup>)  $K_{H2O}$ 

 $K_{H2}$ Adsorption equilibrium constant for H<sub>2</sub> (bar<sup>-1</sup>)

 $K_{15}^{*}$ Equilibrium constant of reaction (15) (dimensionless)

 $K_{16}^{*}$ Equilibrium constant of reaction (16) (dimensionless)

Т Temperature (°C, K)

Universal gas constant (J mol<sup>-1</sup> K<sup>-1</sup>, kcal mol<sup>-1</sup> K<sup>-1</sup>, L atm mol<sup>-1</sup> K<sup>-1</sup>) R

Site where CO and CO<sub>2</sub> adsorb competitively (dimensionless)  $S_1$ 

Site where H<sub>2</sub> and H<sub>2</sub>O adsorb competitively (dimensionless)  $S_2$ 

Adsorption equilibrium constant for CO (bar<sup>-1</sup>) Kco

Adsorption equilibrium constant for CO<sub>2</sub> (bar<sup>-1</sup>)  $K_{CO2}$ 

Parcial fugacity of component i (bar)  $f_i$ 

Pre-exponential factor (atm<sup>-1</sup> h<sup>-1</sup>)  $k_{1,0}$ 

$E_{a,1}$	Apparent activation energy of RWGS reaction (kJ mol <sup>-1</sup> , kcal mol <sup>-1</sup> )
W	Catalyst mass (kg, g)
Fi	Molar flow rate of component i (mol s <sup>-1</sup> , mol h <sup>-1</sup> )
$R_i$	Generation or consumption rate of component i per mass of catalyst (mol s <sup>-1</sup> kg <sup>-1</sup> )
dW	Catalyst mass element (kg)
$V_{\dot{l}}$	Stoichiometric coefficient of component i in the RWGS reaction (dimensionless)
m	Dimensionless mass
$W_0$	Total catalyst mass used in the experiment (kg, g)
<b>y</b> i	Molar fraction of component i in the gas phase (dimensionless)
Р	Pressure (Pa, atm, bar)
Α	Dimensionless parameter A
В	Dimensionless parameter B
D	Dimensionless parameter D
Е	Dimensionless parameter E
G	Dimensionless parameter G
Н	Dimensionless parameter H
1	Dimensionless parameter I
J	Dimensionless parameter J
L	Dimensionless parameter L
N	Dimensionless parameter N
Q	Dimensionless parameter Q
q	Volumetric flow rate (m³ s⁻¹, mL min⁻¹, L h⁻¹)
$f_P$	Correction factor for pressure (bar Pa <sup>-1</sup> )
$f_{obj}$	Objective function (dimensionless)

X<sub>CALC</sub> Calculated CO<sub>2</sub> conversion (dimensionless)

X<sub>EXP</sub> Experimental CO<sub>2</sub> conversion (dimensionless)

X CO<sub>2</sub> conversion (dimensionless)

 $\Delta G_R$  Gibbs free energy of reaction (J mol<sup>-1</sup>)

 $\Delta G^{\circ}_{R}$  Standard Gibbs free energy of reaction (J mol<sup>-1</sup>)

 $\Delta H^{\circ}_{R}$  Standard enthalpy of reaction (J mol<sup>-1</sup>)

R<sup>2</sup> Coefficient of determination (dimensionless)

V Volume (m³, L)

n Number of moles (mol)

F<sub>T</sub> Total molar flow rate (mol s<sup>-1</sup>, mol h<sup>-1</sup>)

X<sub>eq</sub> CO<sub>2</sub> conversion at equilibrium (dimensionless)

P<sup>0</sup><sub>i</sub> Partial pressure of component i at the inlet (atm)

P<sup>eq</sup><sub>i</sub> Partial pressure of component i at equilibrium (atm)

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### INTRODUCTION

In recent decades, our planet has been passing through a series of climate changes, associated with rising sea levels, global average temperatures, and ocean acidification (United States Global Change Research Program, 2017). According to the Intergovernmental Panel on Climate Change (IPCC) in its Sixth Assessment Report on Climate Change (2023), the planet's temperature increased between 1970 and 2020 at a rate greater than in any other 50-year period in at least the last two millennia. From 2013 to 2022, the global surface temperature was approximately 1.15 °C above that corresponding to the period between 1850 and 1900 (IPCC, 2023). The 2023 year was confirmed as the hottest on record (Poynting; Rivault, 2024), exceeding the average pre-industrial level by 1.48 °C, as attested at the beginning of 2024 by the European Center for Medium-Range Weather Forecasts (ECMWF).

Such observed warming has been caused by anthropogenic action, mainly due to the progressive greenhouse gases concentration increasing in the Earth's atmosphere (IPCC, 2023). Without the greenhouse effect, the global average temperature would be -18 °C, making life unfeasible on the planet (Casagrande; Silva Junior; Mendonça, 2011; Ambrizzi *et al.*, 2021). Nevertheless, climate system changes, driven by greenhouse gases emissions from human activities, have manifested themselves through the frequency and magnitude of extreme weather events, representing a risk to humanity (IPCC, 2023).

 $CO_2$  accounts for the majority of anthropogenic greenhouse gas emissions, with 74.1% by mass; in second place comes  $CH_4$ , with 17.3%, followed by  $N_2O$  (6.2%) and fluorinated gases (2.4%) (Climate Watch, 2022a). For this reason, reducing  $CO_2$  emissions becomes an urgent need (Shekari *et al.*, 2023). In order to achieve this goal, three main alternatives arise.

The first option involves reducing the amount of CO<sub>2</sub> produced, which requires improvements in energy efficiency and prioritization of less carbon-intensive energy sources, such as renewable energy and hydrogen, to the detriment of burning fossil fuels. This complete change represents a difficult challenge to be met on a time scale of at least decades (Ghodoosi; Khosravi-Nikou; Shariati, 2017; Pöhlmann; Jess, 2016; Ravanchi; Sahebdelfar, 2021; Okonkwo; Yablonsky; Biswas, 2020; Pérez-Alonso *et al.*, 2008). The second option involves CO<sub>2</sub> Capture and Storage (CCS),

which consists of CO<sub>2</sub> separation and its transporting to remote locations for subsequent long-term storage, in order to avoid its release into the atmosphere (Ghodoosi; Khosravi-Nikou; Shariati, 2017; Ateka et al., 2022; Wang et al., 2022; Oshima et al., 2014; Suescum-Morales; Jiménez; Fernández-Rodríguez, 2022; Tawalbeh et al., 2023; Elsernagawy et al., 2020; Ravanchi; Sahebdelfar, 2021; Daza et al., 2016; Pöhlmann; Jess, 2016). The CCS strategy has already proven itself technically viable, with the potential to mitigate global CO<sub>2</sub> emissions by nearly 20% until 2050 (Kamkeng et al., 2021; Suescum-Morales; Jiménez; Fernández-Rodríguez, 2022; Tawalbeh et al., 2023; Cao et al., 2020; Daza; Kuhn, 2016). Nonetheless, as CCS develops, it will be progressively restricted by the existence of natural safe storage alternatives (Pahija et al., 2022). Besides, these technologies have high energy consumption (which could result in even more emissions) and a high cost of investment, transport and storage, which makes their commercial implementation on a large scale difficult and curbs their contribution to mitigating climate change (Kamkeng et al., 2021; Cao et al., 2020; Kaiser et al., 2013; Daza; Kuhn, 2016) Therefore, CCS by itself is unable to reduce carbon dioxide emissions (Pahija et al., 2022). The third option is the capture and usage of CO<sub>2</sub> (approach commonly abbreviated as CCU, an acronym for Carbon Capture and Utilization) (Ghodoosi; Khosravi-Nikou; Shariati, 2017; Shekari et al., 2023; Suescum-Morales; Jiménez; Fernández-Rodríguez, 2022; Pöhlmann; Jess, 2016). Similarly, as in CCS, CCU aims to capture CO<sub>2</sub> from several sources (e.g. industries and power plants) and to avert its emission (Ravanchi; Sahebdelfar, 2021). However, in CCU carbon dioxide is employed as feedstock for processes that transform it into different compounds (Kaiser et al., 2013; Ravanchi; Sahebdelfar, 2021). Thereby, in addition to acting on climate change mitigation, CCU utilizes the hugely plentiful CO<sub>2</sub> to obtain value-added products, such as alcohols, aromatics, olefins and fuels (Suescum-Morales; Jiménez; Fernández-Rodríguez, 2022; Daza; Kuhn, 2016; Nezam et al., 2021). The fact that such an approach provides a continuous supply of carbon-based compounds, generating profitability and minimizing the depletion of fossil fuels, has attracted the attention of researchers in catalysis, process design and materials (Daza et al., 2016; Okonkwo; Yablonsky; Biswas, 2020; Nezam et al., 2021). For this reason, the term CCS gave way to CCUS (Carbon Capture, Utilisation and Storage) in which the economic value of captured CO<sub>2</sub> is enhanced by its application (Kamkeng et al., 2021).

Since the beginning of the millennium, the energy sector's share of global greenhouse gas emissions has remained above 70% (Climate Watch, 2022b); the report The Oil and Gas Industry in Net Zero Transitions (2023), published by the International Energy Agency (IEA), states that, of the total emissions corresponding to this sector, in turn, almost 15% originate from oil and gas production, transport and processing. To transform this reality, Carbon Capture, Utilization, and Storage technologies represent a valuable tool for the oil and gas industry, being a source of opportunities both in financial and technological terms, as emphasized by the Brazilian Oil and Gas Institute in its publication Carbon Capture and Storage Technologies (CCUS) and its Importance for the Energy Transition in Brazil (IBP, 2023).

Meanwhile,  $CO_2$  is a linear molecule in which the four carbon electrons are involved in covalent double bonds with oxygen atoms. Due to the strength of these bonds between oxygen and carbon, the carbon dioxide molecule is characterized by high stability and an intrinsic thermodynamic inertia that makes its direct conversion difficult (Kamkeng *et al.*, 2021; Liu *et al.*, 2017; Su *et al.*, 2017). On the other hand,  $H_2$  is considered a high-energy electron donor, and its standard Gibbs free energy ( $\Delta G^{\circ}_{298 \text{ K}}$  ( $H_2$ ) = 0) is higher than that of  $CO_2$  ( $\Delta G^{\circ}_{298 \text{ K}}$  ( $CO_2$ ) = -394.389 kJ mol<sup>-1</sup>), thus carbon dioxide can be activated through its reduction by  $H_2$  (Dai *et al.*, 2017; Kamkeng *et al.*, 2021; Chase, Jr., 1998). This fact may explain the broad interest in the catalytic hydrogenation of  $CO_2$  as a promising way to provide added value to  $CO_2$ , through the production of a variety of products, including carbon monoxide ( $CO_2$ ), much more reactive than  $CO_2$  (Desgagnés; Iliuta, 2023; Braga; Vidinha; Rossi, 2020; Liu *et al.*, 2020a; Bahmanpour *et al.*, 2020; Su *et al.*, 2017). CO is a building block widely used in the chemical industry to obtain fuels, polymers, chemicals, and hydrocarbons (Desgagnés; Iliuta, 2023; Pahija *et al.*, 2022).

Examples of hydrogenation reactions comprise methanation, reverse watergas shift (RWGS), and methanol synthesis. Among them, the RWGS reaction emerges as the most attractive approach, being an essential intermediate stage in the direct thermochemical CO<sub>2</sub> conversion processes (Dai *et al.*, 2017; Su *et al.*, 2017; Liu *et al.*, 2020b; Chen *et al.*, 2020). In the RWGS reaction, carbon dioxide reacts with hydrogen, thus generating water and carbon monoxide, as shown in equation (1):

$$H_2 + CO_2 \rightleftharpoons CO + H_2O \tag{1}$$

The chemical equilibrium of this reaction is pressure-independent, and therefore capable of operating at atmospheric pressure, reducing investment and operational costs without compromising carbon monoxide yield (Desgagnés; Iliuta, 2023; Chen *et al.*, 2020; Bown *et al.*, 2021). CO, in turn, can be employed in a mixture with H<sub>2</sub> (denominated synthesis gas, or "syngas"), as a reagent in methanol, ethanol, dimethyl ether, and Fischer-Tropsch fuels production (Bown *et al.*, 2021; Gandara-Loe *et al.*, 2021; Liu *et al.*, 2020b). Hence, the RWGS reaction stands out as an interesting option in Carbon Capture, Utilization, and Storage, allowing, more practically and effectively, the transition of CO<sub>2</sub> to added value products as hydrocarbon chains (Chen *et al.*, 2020; Chen *et al.*, 2021; Gandara-Loe *et al.*, 2021; Su *et al.*, 2017).

Despite this, the RWGS reaction still has some problems to overcome before establishing itself as an industrial-scale CCUS alternative. As a result of the low chemical reactivity of CO<sub>2</sub>, its conversion processes have a high energy activation to be surpassed (Liu *et al.*, 2017; Kamkeng *et al.*, 2021; Gandara-Loe *et al.*, 2021). Furthermore, this reaction is moderately endothermic (ΔH°<sub>R, 298 K</sub> = +41.2 kJ mol<sup>-1</sup>), being thermodynamically favored at elevated temperatures, necessary for the cleavage of the chemical bonds between carbon and oxygen (Desgagnés; Iliuta, 2023; Liu *et al.*, 2020a; Liu *et al.*, 2020b; Gandara-Loe *et al.*, 2021). Whereas a lower reaction temperature allows for lower capital costs and energy expenditures, it is essential to develop ways to operate the process under these conditions (Braga; Vidinha; Rossi, 2020; Su *et al.*, 2017). However, CO methanation and Sabatier reaction are instances of side reactions that can take part under similar reaction conditions, competing with RWGS for the available H<sub>2</sub> (Gandara-Loe *et al.*, 2021). In this case, the exothermic nature of these reactions favors them to occur at low temperatures (Gandara-Loe *et al.*, 2021; Liu *et al.*, 2020a).

There is a clear need to design catalysts that are not only highly active, in order to allow the use of the RWGS reaction at lower temperatures, but also highly selective to carbon monoxide, in addition to presenting availability and low cost, ensuring a commercially viable large-scale process (Bown *et al.*, 2021; Gandara-Loe *et al.*, 2021; Kamkeng *et al.*, 2021). To achieve this purpose, it is necessary to

acquire greater knowledge about the RWGS reaction mechanism and its kinetic over commercial and novel catalysts (Su *et al.*, 2017).

However, even for commercial catalysts, the availability of kinetic studies of RWGS reaction is scarce. This is closely related to the fact that the production of a kinetic study is a difficult and time-consuming process that requires dozens – or even hundreds – of experiments, using several different combinations of operating conditions. Still, the scope of accuracy of the kinetic parameters provided by these studies is limited by the range of conditions used, especially with regard to temperature. This path would be greatly facilitated if it were possible to extract kinetic data from light-off curves. If the kinetic parameters could be obtained from the CO<sub>2</sub> conversion data along a temperature ramp (light-off curves), this process would be quite facilitated experimentally, because the number of tests required would be much smaller. In addition, this could enhance the accuracy of the model due to the large number of temperatures evaluated.

In this context, the present work aims to study the performance of the commercial catalyst CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> in the RWGS reaction and carry out a kinetic study, in order to obtain parameter values for reaction rate expressions available in the literature that provides a satisfactory adjust to the experimental data (light-off curves). This information is expected to provide more tools for increasing the degree of maturity of the RWGS technology, taking into account the trade-off between energy demands and thermodynamic restraints of the reaction, thus contributing to decarbonization efforts (Dai *et al.*, 2018; Galhardo *et al.*, 2021).

### 1 LITERATURE REVIEW

### 1.1 Catalysts for RWGS reaction

Catalysts used in heterogeneous catalysis for the RWGS reaction consist typically of well-dispersed metals supported on high surface area metal oxides (Villora-Picó *et al.*, 2024; Zhang *et al.*, 2022). Regarding the metal sites, literature reports both noble metals (Pt, Pd, Rh, Ru, Au) and non-noble metals (Fe, Mo, Cu, Co, Ni) (Bown *et al.*, 2021; Zhang *et al.*, 2022).

Noble metal catalysts have been widely investigated in RWGS reaction, presenting high activity and selectivity, and higher reaction rates (Su *et al.*, 2017; González-Castaño; Dorneanu; Arellano-García, 2021). Nevertheless, these metals are relatively scarce, and their costs are elevated, hindering the application of such materials for large-scale CO<sub>2</sub> utilization (Su *et al.*, 2017; Vu *et al.*, 2022; Bown *et al.*, 2021). In this sense, several efforts have been invested in the design and study of catalysts that present good catalytic performance and cost-effectiveness, an issue in which non-noble metals have shown to be promising alternatives (Su *et al.*, 2017; Vu *et al.*, 2022; González-Castaño; Dorneanu; Arellano-García, 2021).

Nickel is also an economical and highly active non-noble metal (Chen *et al.*, 2021). These features, together with its well-doing on the forward water-gas shift (WGS) reaction, make this material a focus of wide interest for studies of the RWGS reaction (Liu *et al.*, 2020a). Wolf, Jess, and Kern (2016) used a commercial steam reforming catalyst (Ni-Al<sub>2</sub>O<sub>3</sub>) and obtained CO<sub>2</sub> conversions close to equilibrium, observing considerable stability at 900 °C. With a Ni/CeO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> catalyst, Yang *et al.* (2018) obtained CO<sub>2</sub> conversions above 60% at temperatures from 600 °C onwards. Conversely, Ni-based catalysts are also known to face problems such as the deactivation by coke deposition and the occurrence of undesired methanation reactions, (2) and (3) (Chen *et al.*, 2021; Lalinde *et al.*, 2020). These reactions are exothermic ( $\Delta$ H°<sub>R, 298 K</sub> = -165.0 kJ mol<sup>-1</sup> for reaction (2) and  $\Delta$ H°<sub>R, 298 K</sub> = -206.1 kJ mol<sup>-1</sup> for reaction (3)), thus an elevated selectivity toward CH<sub>4</sub> is favored at low temperatures (particularly below 500 °C), more than with noble metals (Vu *et al.*, 2022; Reinikainen *et al.*, 2022; Meng *et al.*, 2018).

$$4 H_2 + CO_2 \rightleftharpoons CH_4 + 2 H_2 O \tag{2}$$

$$3H_2 + CO \rightleftharpoons CH_4 + H_2O \tag{3}$$

Some of the properties that make Fe-based catalysts reputed among the most successful at high temperatures include good adsorption of intermediates, sintering tolerance, thermal stability, and elevated oxygen mobility (Kamkeng *et al.*, 2021; Pastor-Pérez *et al.*, 2017). In the literature, iron is described as an active metal capable of providing reasonable CO<sub>2</sub> conversions and CO selectivities (González-Castaño; Dorneanu; Arellano-García, 2021). Chou, Loiland, and Lobo (2019) studied an unsupported iron catalyst derived from magnetite (Fe<sub>2</sub>O<sub>3</sub>) between 450 °C and 500 °C at atmospheric pressure, obtaining elevated CO formation rate and stability, in addition to selectivity greater than 99% under a 1:1 H<sub>2</sub>/CO<sub>2</sub> ratio. Under low temperature (150 °C), Yamaoka *et al.* (2024) investigated a series of Fe-supported catalysts (Fe/CeO<sub>2</sub>, Fe/Ce<sub>0.5</sub>Zr<sub>0.5</sub>O<sub>2</sub> and Fe/Ce<sub>0.4</sub>Al<sub>0.1</sub>Zr<sub>0.5</sub>O<sub>2</sub>) with an electric field, reporting high CO<sub>2</sub> conversions and selectivities of about 100%.

On the other hand, Cu-based catalysts still stand out as the most studied for the RWGS reaction, being reported as highly active, selective, and cost-effective catalysts, with promising potential to replace noble metals (Vu et al., 2022; Reinikainen et al., 2022; Reina; Odriozola; Arellano-Garcia, 2021). In fact, copper catalysts achieve high CO<sub>2</sub> conversions without CH<sub>4</sub> formation, in addition to being more suitable than iron catalysts for operating at low temperatures (Chen et al., 2021; Kamkeng et al., 2021). Pahija et al. (2022) described copper as an abundant metal with an affinity for CO<sub>2</sub> and H<sub>2</sub> adsorption. Moreover, copper catalysts have already commercial applications in WGS and methanol synthesis processes and have shown great stability under high carbon dioxide concentrations (Su et al., 2017; Elsernagawy et al., 2020). At high temperatures, however, copper nanoparticles tend to sinter (Reina; Odriozola; Arellano-Garcia, 2021). Another issue is the oxidation of part of the metallic Cu by CO<sub>2</sub>, causing agglomeration with consequent loss of metal surface area and, therefore, activity and stability over time (Reina; Odriozola; Arellano-Garcia, 2021; Liu et al, 2020b; Bown et al., 2021). Consequently, research have been directed to enhance the activity and stability of copper RWGS catalysts (Reina; Odriozola; Arellano-Garcia, 2021; Liu et al, 2020b). Some of the strategies employed in this regard include dispersion of the active copper on several supports, search for improvement of parameters that influence catalytic performance (such as morphology, Cu content, and surface area), and use of promoters (Reina; Odriozola; Arellano-Garcia, 2021).

Chen, Cheng, and Lin (2004) studied the RWGS reaction over Cu/SiO<sub>2</sub> catalysts under H<sub>2</sub>/CO<sub>2</sub> flow in a 1:1 ratio, concluding that the addition of a small amount of iron as a promoter (0.3% Fe to 10% Cu/SiO<sub>2</sub>) was enough to upgrade the performance and stability appreciably. The catalyst presented an elevated conversion, at 600 °C and atmospheric pressure, for over 120 h without deactivation (Chen; Cheng; Lin, 2004). Ai *et al.* (2022) prepared supported Cu/γ-Al<sub>2</sub>O<sub>3</sub> by wet impregnation and by grinding, achieving a reaction rate of 1.85·10<sup>-5</sup> mol g<sub>cat</sub><sup>-1</sup> s<sup>-1</sup> with the catalyst made by wet impregnation and a reaction rate of 2.12·10<sup>-5</sup> mol g<sub>cat</sub><sup>-1</sup> s<sup>-1</sup> for the catalyst obtained by the grinding method. The authors reported that the grinding method provided higher content and dispersion of metallic Cu on the surface of the catalyst (Ai *et al.*, 2022).

Jurković *et al.* (2017) investigated the effect of the support on Cu-based catalysts, analyzing Al<sub>2</sub>O<sub>3</sub>, CeO<sub>2</sub>, SiO<sub>2</sub>, TiO<sub>2</sub>, and ZrO<sub>2</sub>. All the catalysts were prepared by deposition-precipitation method and evaluated in the temperature range from 280 °C to 360°C (Jurković *et al.*, 2017). Alumina was reported to be the support that provides the highest Cu dispersion, and also the greatest catalyst activity (Jurković *et al.*, 2017). There is a linear dependence between activity and surface area of Cu<sup>0</sup>, thereby this oxide may boost the reaction rate (Su *et al.*, 2017).

Cu-based catalysts are also widely used in conjunction with ZnO. In these catalysts, copper acts as the main active metal, while zinc is a promoter; the interface between CuO and ZnO plays a pivotal role in the proceeding of the reaction, therefore it is essential to choose a preparation method that provides a good dispersion of the phases on the catalyst surface (Jurković *et al.*, 2017). ZnO supplies active sites for hydrogen spillover, in addition to influencing Cu<sup>0</sup> dispersion (Reina; Odriozola; Arellano-Garcia, 2021). The performance is described in the literature as being better for samples with greater Cu content (Jurković *et al.*, 2017; Su *et al.*, 2017; Ai *et al.*, 2022). Besides, ZnO shows more efficiency in the presence of other oxides such as alumina and zirconia (Reina; Odriozola; Arellano-Garcia, 2021).

 $\text{Cu/Al}_2\text{O}_3$  and  $\text{Cu/ZnO/Al}_2\text{O}_3$  are often used in RWGS due to their attractive price, as well as good activity and selectivity to CO at low temperatures (between 170 – 250 °C) (Vu *et al.*, 2022; Elsernagawy *et al.*, 2020). The high surface area of

alumina makes CuO and ZnO crystallite size smaller, and the copper dispersion is also favored for higher Cu/Zn ratios (Reina; Odriozola; Arellano-Garcia, 2021; Stone; Waller, 2003). Jadhav, Joshi and Vaidya (2020) synthesized Cu/ZnO/Al<sub>2</sub>O<sub>3</sub> catalysts by hydrothermal and combustion methods, testing the samples in a temperature range from 280 °C to 300 °C and H<sub>2</sub>/CO<sub>2</sub> ratio of 3. In all cases, no coke formation was observed, and the authors concluded that the catalyst prepared by the hydrothermal technique was more stable than that obtained by the combustion technique, with the former providing a consistent activity for the 20 h of the test, because of the ability of the hydrothermal method to provide catalysts with strongly crystalline nature (Jadhav; Joshi; Vaidya; 2020).

### 1.2 RWGS mechanism

In order to design more effective catalysts, it is important to clarify the elementary steps of RWGS over catalytic surface (Su *et al.*, 2017; González-Castaño; Dorneanu; Arellano-García, 2021). Several in-situ techniques and density functional theory (DFT) calculations have provided kinetic data that supports the search for a deeper understanding of the RWGS pathway, still a subject under discussion (Pahija *et al.*, 2022; Su *et al.*, 2017; Ateka *et al.*, 2022; González-Castaño; Dorneanu; Arellano-García, 2021). For the reaction, there are two categories of mechanisms usually accepted: the surface redox mechanism and the associative mechanism (Gu *et al.*, 2021; Liu *et al*, 2020a; Chen *et al.*, 2020). These pathways differ mainly regarding the participation or not of the dissociated H<sub>2</sub> in the production of carbonaceous intermediates (Chen *et al.*, 2020; Su *et al.*, 2017; González-Castaño; Dorneanu; Arellano-García, 2021).

In the redox mechanism (also called dissociative or regenerative mechanism), CO<sub>2</sub> dissociates to CO, oxidizing the metal (González-Castaño; Dorneanu; Arellano-García, 2021; Reina; Odriozola; Arellano-Garcia, 2021). Next, H<sub>2</sub> reduces the active site to its initial state (Pahija *et al.*, 2022; González-Castaño; Dorneanu; Arellano-García, 2021). The H species does not take part in CO<sub>2</sub> dissociation (González-Castaño; Dorneanu; Arellano-García, 2021). The redox mechanism requires two key conditions: the catalyst surface must be able to be reduced by H<sub>2</sub> and, once partially

reduced, it must be able to be efficiently reoxidized by CO<sub>2</sub> at RWGS conditions (Reina; Odriozola; Arellano-Garcia, 2021).

The redox mechanism was originally described over Cu-based catalysts, as indicated below (Chen *et al.*, 2020; Ginés; Marchi; Apesteguía, 1997; Reina; Odriozola; Arellano-Garcia, 2021; Zhu; Ge; Zhu, 2020):

$$CO_{2(g)} + 2Cu_{(s)}^{0} \rightarrow CO_{(g)} + Cu_{2}O_{(s)}$$
 (4)

$$H_{2(g)} + Cu_2O_{(s)} \rightarrow H_2O_{(g)} + 2Cu_{(s)}^0$$
 (5)

Cu<sup>0</sup> is the active site that facilitates the dissociation of CO<sub>2</sub> and undergoes consecutive oxidation and reduction by carbon monoxide and hydrogen, respectively (Chen *et al.*, 2020; Ginés; Marchi; Apesteguía, 1997; Reina; Odriozola; Arellano-Garcia, 2021). This scheme shows CO<sub>2</sub> oxidizing metallic copper, forming Cu<sup>+</sup> and carbon monoxide, while H<sub>2</sub> reduces Cu<sup>+</sup> to Cu<sup>0</sup>, originating water (Chen *et al.*, 2020).

Ginés, Marchi, and Apesteguía (1997) carried out a kinetic study over CuO/ZnO/Al<sub>2</sub>O<sub>3</sub>, corroborating this mechanism. Online gas analysis during CO<sub>2</sub>/H<sub>2</sub> cycles at 230 °C and 1 atm showed that the CO<sub>2</sub> addition to the reactor generated only CO. Further addition of H<sub>2</sub> to the reactor generated only water. Furthermore, through quantitative gravimetric data, the authors found that the catalyst weight gain after the introduction of the CO<sub>2</sub>-containing atmosphere represented an atomic ratio of around 0.4-0.5 between the oxygen and the copper on the surface, which is a likely value in agreement with the reaction (4). This suggests a coverage of adsorbed oxygen atoms on the copper surface of 50%. Moreover, the weight gain was also almost equal to the weight loss of the catalyst during the subsequent introduction of H<sub>2</sub>. The authors still detailed the mechanism through the reactions (6) to (10), assuming active sites are identical and no interaction between adsorbed species:

$$CO_{2(g)} + 2S \rightleftharpoons CO_{(a)} + O_{(a)}$$
 (6)

$$CO_{(a)} \rightleftharpoons CO_{(g)} + S \tag{7}$$

$$H_{2(g)} + 2S \rightleftharpoons 2H_{(a)}$$
 (8)

$$2 H_{(a)} + O_{(a)} \rightleftharpoons H_2 O_{(a)} + 2 S \tag{9}$$

$$H_2O_{(a)} \rightleftharpoons H_2O_{(g)} + S$$
 (10)

where S represents the vacant active sites, and the subscript (a) denotes adsorbed species. In the same work, the authors ruled out possible support effects on hydrogen chemisorption after observing that  $H_2$  chemisorption in  $Al_2O_3$  and ZnO samples at 230 °C was negligible, indicating selective adsorption in the metallic copper phase (Ginés; Marchi; Apesteguía, 1997). The dissociative adsorption of  $CO_2$  is the rate-determining step under  $H_2$ -rich conditions, whereas, at  $H_2$ -lean conditions, both the  $CO_2$  dissociation and the water formation are rate-determining steps (Ginés; Marchi; Apesteguía, 1997).

In the associative mechanism, CO<sub>2</sub> adsorbs on the surface of the catalyst, reacts with adsorbed H from the previous dissociative adsorption of H<sub>2</sub>, and produces intermediate species like carboxyl and formate (Gu *et al.*, 2021; Pahija *et al.*, 2022). Whatever the intermediate species, it decomposes to produce CO and H<sub>2</sub>O (Gu *et al.*, 2021; Pahija *et al.*, 2022; Chen *et al.*, 2020). In this case, CO<sub>2</sub> adsorption and H<sub>2</sub> dissociation are found the essential elementary steps (Gu *et al.*, 2021).

In the formate-mediated mechanism, a formate intermediate species,  $HCOO_{(a)}$ , is generated through a hydrogenation of the adsorbed carbon dioxide, dissociating instantaneously. The reaction can be explained by the following scheme (Chen *et al.*, 2020):

$$H_{2(g)} + 2S \rightleftharpoons 2H_{(a)} \tag{8}$$

$$CO_{2(g)} + S \rightleftharpoons CO_{2(a)} \tag{11}$$

$$CO_{2(a)} + H_{(a)} \rightleftharpoons HCOO_{(a)} + S$$
 (12)

$$HCOO_{(a)} + S \rightleftharpoons HCO_{(a)} + O_{(a)}$$
 (13)

$$HCO_{(a)} + S \rightleftharpoons CO_{(a)} + H_{(a)} \tag{14}$$

$$H_{(a)} + O_{(a)} \rightleftharpoons OH_{(a)} + S$$
 (15)

$$H_{(a)} + OH_{(a)} \rightleftharpoons H_2O_{(a)} + S$$
 (16)

$$H_2 O_{(a)} \rightleftharpoons H_2 O_{(g)} + S$$
 (17)

$$CO_{(a)} \rightleftharpoons CO_{(g)} + S \tag{18}$$

In the carboxyl-mediated mechanism, a carboxyl intermediate species,  $COOH_{(a)}$ , is formed as shown in reactions (8), (11) and (19), with H assisting the dissociation of the C–O bond, and the carboxyl instantly decomposes into CO,

sequence that can take place through two different pathways, being one described by the following scheme (Chen *et al.*, 2020):

$$H_{2(q)} + 2S \rightleftharpoons 2H_{(q)}$$
 (8)

$$CO_{2(g)} + S \rightleftharpoons CO_{2(a)} \tag{11}$$

$$CO_{2(a)} + H_{(a)} \rightleftharpoons COOH_{(a)} + S$$
 (19)

$$COOH_{(a)} + S \rightleftharpoons CO_{(a)} + OH_{(a)}$$
 (20)

$$H_{(a)} + OH_{(a)} \rightleftharpoons H_2O_{(a)} + S$$
 (16)

$$H_2O_{(a)} \rightleftharpoons H_2O_{(g)} + S$$
 (17)

$$CO_{(a)} \rightleftharpoons CO_{(g)} + S \tag{18}$$

The other proposed pathway is presented below (Chen et al., 2020):

$$H_{2(g)} + 2S \rightleftharpoons 2H_{(a)}$$
 (8)

$$CO_{2(g)} + S \rightleftharpoons CO_{2(a)} \tag{11}$$

$$CO_{2(a)} + H_{(a)} \rightleftharpoons COOH_{(a)} + S$$
 (19)

$$COOH_{(a)} + S \rightleftharpoons HCO_{(a)} + O_{(a)}$$
 (21)

$$HCO_{(a)} + S \rightleftharpoons CO_{(a)} + H_{(a)}$$

$$\tag{22}$$

$$H_{(a)} + O_{(a)} \rightleftharpoons OH_{(a)} + S$$
 (15)

$$H_{(a)} + OH_{(a)} \rightleftharpoons H_2O_{(a)} + S$$
 (16)

$$H_2 O_{(a)} \rightleftharpoons H_2 O_{(g)} + S$$
 (17)

$$CO_{(a)} \rightleftharpoons CO_{(g)} + S \tag{18}$$

It is noteworthy that, in reactions (21) and (22), the  $COH_{(a)}$  intermediate could be found instead of  $HCO_{(a)}$ , although  $COH_{(a)}$  is reported to be less stable than its isomer over several metal surfaces (Chen *et al.*, 2017).

The nature and quantity of formed intermediates vary according to the metal and the support (Reina; Odriozola; Arellano-Garcia, 2021). On reducible supports, the oxygen vacancies might play the role of active sites allowing CO<sub>2</sub> reduction and the C=O bond cleavage (González-Castaño; Dorneanu; Arellano-García, 2021). Temperature can also influence the rate of decomposition of intermediates, leading to different reaction pathways (González-Castaño; Dorneanu; Arellano-García, 2021).

Chen, Cheng and Lin (2000) studied the mechanism of CO formation over  $Cu/Al_2O_3$ , concluding that a redox mechanism could not completely elucidate the reaction pathway. They deduced that  $H_2$  plays a key role in carbon monoxide formation by associating with adsorbed  $CO_2$  to produce reaction intermediates, and proposed formate species as the dominant intermediate.

Dietz, Piccinin and Maestri (2015) carried out DFT calculations on (111) surfaces of Pt, Rh, Ni, Cu, Ag and Pd, demonstrating that the dominant mechanism of the RWGS reaction varies according to the metal, due to the influence of its interaction with oxygen adatom on the activation energy of the dissociation. The authors state that, whereas the dissociation of CO<sub>2</sub> is favored on metals with greater oxygen affinity, CO<sub>2</sub> hydrogenation is favored as the interaction between O and the metal weakens. They also report the preponderance of the surface redox mechanism over Rh, Ni and Cu, and the carboxyl-mediated associative mechanism over Pt, Pd and Ag.

Regardless the sort of the predominant mechanism, an active catalyst for CO<sub>2</sub> reduction must be able to provide the chemisorption of carbon dioxide molecules and cleavage of one of its C–O bonds, as well as dissociation of H<sub>2</sub> with subsequent hydrogenation of O to originate water (González-Castaño; Dorneanu; Arellano-García, 2021; Zhu; Ge; Zhu, 2020; Chen *et al.*, 2020). Nevertheless, for such a catalyst to also be selective, it must present a moderate C–O dissociation capacity and a weak CO adsorption ability, in order to avoid the dissociation of this CO and its eventual additional hydrogenation, causing the formation of methane and methanol (Zhu; Ge; Zhu, 2020). Hence, there is a balance that needs to be achieved between C–O bond dissociation and hydrogenation, allowing the catalyst to not only provide high CO<sub>2</sub> conversions under milder conditions but also be selective toward the desired product. Such properties clearly depend on the characteristics of metals, supports and promoters, as well as the interactions between them (Zhu; Ge; Zhu, 2020).

### 1.3 Thermodynamic and kinetic behavior of the system

An important tool in the design and improvement of the RWGS process, in general, is the thermodynamic analysis, which allows evaluation of the tendency of the reaction to proceed or not, as well as the extent of the reaction at the equilibrium

according to parameters like temperature, pressure and feed composition (Santos *et al.*, 2023).

An excess of H<sub>2</sub> (relative to CO<sub>2</sub>) increases CO<sub>2</sub> conversion at equilibrium (Daza; Kuhn, 2016). The same occurs with increasing temperature, because of the kinetic favoring and the endothermicity of the RWGS reaction (Daza; Kuhn, 2016; Elsernagawy et al., 2020). Furthermore, at lower temperatures, RWGS suffers from competition with methanation (González-Castaño; Dorneanu; Arellano-García, 2021; Pastor-Pérez et al., 2017). Despite this, from a practical point of view, it is well-known that higher temperatures result in higher energy consumption and higher capital cost, in addition to being potentially harmful to catalysts (González-Castaño; Dorneanu; Arellano-García, 2021; Su et al., 2017). Similarly, to work with higher H<sub>2</sub>/CO<sub>2</sub> molar ratios in the feed, a greater quantity of hydrogen is required, which is the most expensive raw material in the process (Santos et al., 2023). In the same way, the decrease in space velocity represents an increase in residence time that is expected to provide higher conversions, but it is also associated with larger reactor volumes, resulting in an expressive rise in capital cost (Pastor-Pérez et al., 2017). Regarding total pressure, a substantial effect on the equilibrium composition is not expected for the RWGS reaction, because the number of moles is the same for the products and reactants, as seen in reaction (1). However, the methanation reactions (2) and (3), which are volume contraction processes, are favored by an increase in pressure (Bulfin et al., 2023).

Santos *et al.* (2023) simulated RWGS reaction in ASPEN Plus (v10.0) and investigated the response to different operation conditions (Annex, Figure 18). At 1 bar with a 1:1 H<sub>2</sub>/CO<sub>2</sub> molar ratio for the inlet stream, it was observed that CH<sub>4</sub> is the predominant product below 520 °C. CO assumes this position above 700 °C, and from 825 °C the molar fraction of this compound in the product stream is higher than that of CO<sub>2</sub> and H<sub>2</sub>. Regarding the feed molar ratio (H<sub>2</sub>/CO<sub>2</sub>), a range between 0.5 and 1.5 was evaluated. CO<sub>2</sub> conversion was higher above 1.2 but CO selectivity increased above 0.8. Therefore, 0.8 was considered the appropriate value for the molar ratio to contribute to better cost-effectiveness. The authors also remarked on the negative effect of pressure on the CO concentration downstream. Even so, they proposed 20 bar as a suitable pressure for the process, because the desired selectivity can be obtained with an appropriate catalyst. Besides, such pressure is

commercially employed for FTS (Fischer-Tropsch Synthesis) and can facilitate the integration between these processes.

Utilizing the software ASPEN Plus (v10.0), Elsernagawy *et al.* (2020) carried out a thermo-economic analysis through a steady-state simulation of RWGS reaction followed by methanol synthesis both at higher (940 °C) and lower (450 °C) temperatures. A Cu-ZnO/Al<sub>2</sub>O<sub>3</sub> was considered for a lower temperature approach, and Ni/Al<sub>2</sub>O<sub>3</sub> was considered for operating at higher temperatures. The results showed that the performance of both approaches was quite similar. Although the lower temperature corresponded to lower energy consumption, this approach required higher recycling ratios, and thus bigger volumes of reactors and higher amounts of catalyst to reach the same production, increasing the production cost. On the other hand, the higher temperature approach presented a better environmental performance evidenced by a larger negative carbon footprint, and was considered more advantageous. The authors further explored the effect of the H<sub>2</sub>/CO<sub>2</sub> ratio at 500 °C and 10 bar, finding an optimal feed ratio of 3:1 due to the higher CO<sub>2</sub> and H<sub>2</sub> conversions obtained under these conditions.

Reinikainen *et al.* (2022) simulated CO<sub>2</sub> conversion in the RWGS reactor as a function of GHSV at 850 °C in the software ASPEN Plus v11 (Annex, Figure 19). They also investigated the effect of H<sub>2</sub>/CO<sub>2</sub> feed ratio, observing that, at the lowest GHSV values, the conversion was quite near to equilibrium. Moreover, the more the space velocity increased, the further the conversions were moved away from equilibrium values. The work also highlighted the strong influence of the inlet H<sub>2</sub>/CO<sub>2</sub> molar ratio on the composition of the product stream, monitoring a range between 1 and 3. A linear dependence of the selectivity to CH<sub>4</sub> concerning the H<sub>2</sub>/CO<sub>2</sub> ratio was observed since methanation consumes the excess hydrogen available in the medium.

#### 1.4 Kinetic studies

In their kinetic study over CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalysts, Ginés, Marchi and Apesteguía (1997) analyzed the RWGS considering a surface redox mechanism, summarized by following reactions, where *S* represents the vacant active sites, and the subscript (a) denotes adsorbed species.

$$CO_{2(q)} + S \rightleftharpoons CO_{(q)} + O_{(a)}$$
 (23)

$$H_{2(g)} + 2S \rightleftharpoons 2H_{(a)}$$
 (8)

$$2H_{(a)} + O_{(a)} \rightleftharpoons H_2O_{(a)} \tag{24}$$

Assuming (23) as the rate-determining step, the authors proposed the reaction rate equation (25), obtained through Langmuir-Hinshelwood kinetics:

$$r_{RWGS} = \frac{k_1 L_0 \left( P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1} \right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_8^* K_{24}^*} \cdot P_{CO}}$$
(25)

in which  $r_{RWGS}$  is the RWGS reaction rate in mol h<sup>-1</sup> g<sup>-1</sup>,  $k_1$  is the forward reaction constant of reaction (23) in atm<sup>-1</sup> h<sup>-1</sup>,  $L_0$  indicates the concentration of active sites of fresh catalyst in mol g<sup>-1</sup>,  $P_i$  represents the partial pressure of component i in atm,  $K_1$  is the equilibrium constant of the RWGS reaction (dimensionless),  $K_8$ \* is the equilibrium constant of the dissociative hydrogen adsorption (8) in atm<sup>-1</sup>, and  $K_{24}$ \* is the equilibrium constant of reaction (24), also in atm.

Vanden Bussche and Froment (1996) developed a steady-state kinetic model for the RWGS reaction over a commercial Cu/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst, also considering a redox mechanism, expressed by the following reactions:

$$H_{2(g)} + 2S \rightleftharpoons 2H_{(a)}$$
 (8)

$$CO_{2(g)} + S \rightleftharpoons CO_{(g)} + O_{(a)}$$
 (23)

$$H_{(a)} + O_{(a)} \rightleftharpoons OH_{(a)} + S$$
 (15)

$$H_{(a)} + OH_{(a)} \rightleftharpoons H_2O_{(a)} + S$$
 (16)

$$H_2 O_{(a)} \rightleftharpoons H_2 O_{(g)} + S$$
 (17)

The authors considered the dissociative adsorption of CO<sub>2</sub> as the ratedetermining step and presented the reaction rate indicated in equation (26):

$$r_{RWGS} = \frac{k_1 \cdot P_{CO_2} \cdot \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{P_{H_2O} \cdot P_{CO}}{P_{CO_2} \cdot P_{H_2}}\right)\right)}{\left(1 + \left(\frac{K_{H_2O}}{K_{15}^* K_{16}^* K_{H_2}}\right) \left(\frac{P_{H_2O}}{P_{H_2}}\right) + \sqrt{K_{H_2} \cdot P_{H_2}} + K_{H_2O} \cdot P_{H_2O}\right)}$$
(26)

where  $r_{RWGS}$  is the reaction rate in mol kg<sup>-1</sup> s<sup>-1</sup>, k<sub>1</sub> the reaction rate constant in mol kg<sup>-1</sup> s<sup>-1</sup> bar<sup>-1</sup>,  $P_i$  the partial pressure of component i in bar,  $K_1$  the RWGS equilibrium constant (dimensionless),  $K_{H2O}$  the adsorption equilibrium constant for H<sub>2</sub>O in bar<sup>-1</sup>,  $K_{H2}$  the adsorption equilibrium constant for H<sub>2</sub> in bar<sup>-1</sup>,  $K_{15}$ \* is the equilibrium constant of reaction (15) (dimensionless) and  $K_{16}$ \* is the equilibrium constant of reaction (16) (dimensionless). Indeed,  $k_1$  is a compounded constant, expressed by equation (27):

$$k_1 = k_{23} \cdot c_t \tag{27}$$

where  $k_{23}$  is the rate constant of reaction (23) and  $c_t$  is the total number of active sites. The equilibrium constant of RWGS reaction,  $K_1$ , is determined through equation (28), from Graaf *et al.* (1986), applicable at low pressures:

$$K_1 = 10^{\left(-\frac{2073}{T} + 2.029\right)} \tag{28}$$

where T is the temperature in K. The other kinetic and adsorption equilibrium constants can be calculated by the equations (29) to (32):

$$k_1 = A_{k_1} \cdot exp\left(\frac{B_{k_1}}{R \cdot T}\right) \tag{29}$$

$$K_{H_2O} = A_{K_{H_2O}} \cdot exp\left(\frac{B_{K_{H_2O}}}{R \cdot T}\right) \tag{30}$$

$$\frac{K_{H_2O}}{K_{15}^* K_{16}^* K_{H_2}} = A_{K_{H_2O}/K_{15}^* K_{16}^* K_{H_2}} \cdot exp\left(\frac{B_{K_{H_2O}/K_{15}^* K_{16}^* K_{H_2}}}{R \cdot T}\right)$$
(31)

$$\sqrt{K_{H_2}} = A_{\sqrt{K_{H_2}}} \cdot exp\left(\frac{B_{\sqrt{K_{H_2}}}}{R \cdot T}\right) \tag{32}$$

where  $A_{k1}$  (mol kg<sup>-1</sup> s<sup>-1</sup> bar<sup>-1</sup>),  $B_{k1}$  (J mol<sup>-1</sup>),  $A_{KH2O}$  (bar<sup>-1</sup>),  $B_{KH2O}$  (J mol<sup>-1</sup>),  $A_{KH2O/K15*K16*KH2}$  (dimensionless),  $A_{\sqrt{KH2}}$  (bar<sup>-0,5</sup>) and  $B_{\sqrt{KH2}}$  (J mol<sup>-1</sup>) are the seven

parameters to be fitted for this model since  $B_{KH2O/K15*K16*KH2}$  is set to zero by the authors and R is the universal gas constant (equal to 8.314 J mol<sup>-1</sup> K<sup>-1</sup>) (NIST, 2024).

Graaf, Stamhuis and Beenackers (1988) studied the kinetics of low-pressure methanol synthesis over a commercial  $Cu/ZnO/Al_2O_3$  catalyst, considering a dual-site adsorption mechanism. On one site (represented as  $S_1$ ), CO and CO<sub>2</sub> adsorb competitively, while, at the other site (represented as  $S_2$ ),  $H_2$  and  $H_2O$  adsorb competitively. They presented the following reaction scheme for RWGS reaction:

$$CO_{2(g)} + S_1 \rightleftharpoons CO_{2(g)} \tag{33}$$

$$H_{2(g)} + 2S_2 \rightleftharpoons 2H_{(a)}$$
 (34)

$$CO_{2(a)} + H_{(a)} \rightleftharpoons HCO_{2(a)} + S_2$$
 (35)

$$HCO_{2(a)} + H_{(a)} \rightleftharpoons CO_{(a)} + H_2O_{(a)}$$
 (36)

$$CO_{(a)} \rightleftharpoons CO_{(g)} + S_1 \tag{37}$$

$$H_2 O_{(a)} \rightleftharpoons H_2 O_{(g)} + S_2$$
 (38)

The authors proposed a rate equation for RWGS reaction, expressed by equation (39):

$$r_{RWGS} = \frac{k_1 \cdot K_{CO_2} \cdot \left( f_{CO_2} \cdot f_{H_2} - \frac{f_{H_2O} \cdot f_{CO}}{K_1} \right)}{\left( 1 + K_{CO} \cdot f_{CO} + K_{CO_2} \cdot f_{CO_2} \right) \left( f_{H_2}^{0.5} + f_{H_2O} \cdot \left( \frac{K_{H_2O}}{K_{H_2}^{0.5}} \right) \right)}$$
(39)

where  $K_i$  is the adsorption equilibrium constant of component i in bar<sup>-1</sup>,  $f_i$  is the partial fugacity of component i in bar,  $K_1$  is the equilibrium constant of RWGS reaction (dimensionless) and  $k_1$  is the rate constant, which contains the adsorption equilibrium constant of hydrogen and is expressed in mol s<sup>-1</sup> kg<sup>-1</sup> bar<sup>-0.5</sup>.

 $K_1$  and  $k_1$  are determined through equations (28) and (29), respectively, while the adsorption equilibrium constants are calculated by equations (40) to (42):

$$K_{CO} = A_{K_{CO}} \cdot exp\left(\frac{B_{K_{CO}}}{R \cdot T}\right) \tag{40}$$

$$K_{CO_2} = A_{K_{CO_2}} \cdot exp\left(\frac{B_{K_{CO_2}}}{R \cdot T}\right) \tag{41}$$

$$\frac{K_{H_2O}}{K_{H_2}^{0.5}} = A_{K_{H_2O}/K_{H_2}^{0.5}} \cdot exp\left(\frac{B_{K_{H_2O}/K_{H_2}^{0.5}}}{R \cdot T}\right)$$
(42)

therefore  $A_{k1}$  (mol s<sup>-1</sup> kg<sup>-1</sup> bar<sup>-0.5</sup>),  $B_{k1}$  (J mol<sup>-1</sup>),  $A_{KCO}$  (bar<sup>-1</sup>),  $B_{KCO}$  (J mol<sup>-1</sup>),  $A_{KCO2}$  (bar<sup>-1</sup>),  $B_{KCO2}$  (J mol<sup>-1</sup>),  $A_{KH2ONKH2}$  (bar<sup>-0.5</sup>) and  $B_{KH2ONKH2}$  (J mol<sup>-1</sup>) are the eight parameters to be fitted for this kinetic model.

#### 1.5 Final considerations

Given all that has been exposed, it is possible to observe that copper-based catalysts represent a promising perspective toward the industrial application of the RWGS reaction. However, the simulations reported in the literature indicated that the RWGS process is favored under conditions generally associated with high investment and operating costs, such as low space velocities, high temperatures, and H<sub>2</sub>/CO<sub>2</sub> ratios. Therefore, it is desirable to develop catalysts that promote the highest possible conversion of CO<sub>2</sub> to the product of interest, carbon monoxide. This objective requires a deeper understanding of how the reaction occurs on the catalytic surface since the reaction mechanism is still a topic under constant discussion. Nevertheless, the development of a new kinetic study can be a very challenging task. The studies in the literature were based on kinetic data obtained in a steady state, requiring at least one catalytic run for each set of operating conditions. Thus, this process demands considerable experimental effort due to the large number of tests, consuming a lot of time and resources.

Furthermore, the accuracy of the original parameters of these models may drop considerably in the case of extrapolation outside the temperature window used. Although there is the possibility that temperature ramp tests may be able to provide kinetic data in less time, in a simpler manner, and cover a wider temperature range, there is a lack of studies in the literature exploring this alternative. Also, no studies were found that compare the accuracy of the estimates provided by the available kinetic models for the RWGS reaction under experimental conditions different from

those employed in its acquisition. Therefore, the present work has the following general objectives:

- a) Study the kinetics of the RWGS reaction on a commercial CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst;
- b) To evaluate the possible use of light-off curves (in temperature ramp) as a replacement for the conventional procedure (in steady state – constant temperature levels) to obtain the kinetic parameters, thus contributing to the development of more effective catalysts for the RWGS reaction.

# The specific objectives are:

- a) Evaluate diffusional effects on the catalytic bed;
- b) Analyze the effect of different experimental conditions on CO<sub>2</sub> conversion through RWGS reaction over a commercial CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst for kinetic studies;
- c) Obtain kinetic parameter values for the RWGS reaction rate expressions present in the literature based on experimental data of CO<sub>2</sub> conversion along a temperature ramp (light-off curves);
- d) Compare the kinetic models of Ginés, Marchi, and Apesteguía (1997), Vanden Bussche and Froment (1996), and Graaf, Stamhuis, and Beenackers (1988) from the point of view of accuracy in modeling the experimental light-off curves;
- e) Compare the fit quality to experimental data of parameters obtained from light-off curves and parameters adjusted by the conventional procedure with steady-state data.

#### 2 METHODOLOGY

# 2.1 Catalyst

The CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> used in this study is a commercial catalyst provided by Prosint (a methanol producer in Brazil that is now out of business). It was calcined at 500 °C for 3 h, at a 10 °C min<sup>-1</sup> rate before use.

## 2.2 Catalyst characterization

X-ray diffraction (XRD) analysis was performed on a Bruker D8 Advance diffractometer employing a  $CuK_{\alpha}$  radiation source. The 20 range employed was 10–70°, scanning speed of 4° min<sup>-1</sup>, step size of 0.02° and step time of 0.3 s. The qualitative analysis of the resulting patterns was accomplished based on the JCPDS database (Joint Committee on Powder Diffraction Standards) and literature information.

Temperature-Programmed Reduction (TPR), with H<sub>2</sub> as the reducing agent (H<sub>2</sub>-TPR), was performed in a Micromeritics AutoChem II 2920 instrument, furnished with a Thermal Conductivity Detector (TCD). 51.6 mg of catalyst were placed into the U-shaped quartz fixed bed reactor. First, the sample was pretreated at 150 °C, with a heating rate of 10 °C min<sup>-1</sup> from room temperature, remaining at this temperature for 10 min, under a 50 mL min<sup>-1</sup> argon flow. After returning to room temperature, the catalyst was reduced under 50 mL min<sup>-1</sup> of 10% H<sub>2</sub>/Ar mixture (ramp of 10 °C min<sup>-1</sup> up to 500 °C).

#### 2.3 Catalytic evaluation

The RWGS catalytic tests were performed at atmospheric pressure in a Pyrex U-shaped fixed bed reactor placed into a multipurpose unit coupled to an Agilent 7890A gas chromatograph equipped with a thermal conductivity detector (TCD), a

front inlet detector (FID), GS – GASPRO and HP – MOLESIEVE capillary column. A catalyst sample of 50 mg was diluted with silicon carbide in a 1:1 mass ratio, in order to increase the thermal homogeneity of the bed, minimize the occurrence of hot spots within the reactor, and thus ensuring the reproducibility of the tests. A pretreatment was carried-out under H<sub>2</sub> flow, at 500 °C (heating rate of 10 °C min<sup>-1</sup>) for 1 h. The following mixtures, with different H<sub>2</sub>/CO<sub>2</sub> molar ratios, were used in the tests: mixture 1 (0.10:0.10, and balance in He), mixture 2 (0.25:0.10, and balance in He) and mixture 3 (0.40:0.10, and balance in He).

#### 2.3.1 <u>Light-off tests</u>

The light-off curve of a catalytic reaction is a plot of conversion versus temperature. These curves are commonly used in catalyst development since they allow evaluating the catalytic activity (Duprat, 2022). Three light-off curves relating CO<sub>2</sub> conversion to reaction temperature were obtained using the three mixtures, with different H<sub>2</sub>/CO<sub>2</sub> molar ratios. In all the experiments, after the pretreatment previously defined, a heating rate of 5 °C min<sup>-1</sup> was applied, from room temperature to 500 °C, with a space velocity of 30 m<sup>3</sup> kg<sup>-1</sup> h<sup>-1</sup>.

The objective of these tests is to generate a large set of kinetic data in a single experiment.

#### 2.3.2 Evaluation of possible diffusional effects

In order to verify whether the contribution of internal mass transfer is significant for the reactor modeling, three temperature ramp tests (light-off tests) were performed with mixture 3 (H<sub>2</sub>/CO<sub>2</sub> molar ratio of 4) at 30 m³ kg⁻¹ h⁻¹. The calcined catalyst was sieved through A Bronzinox sieves to produce three samples (50 mg) with different particle sizes in the ranges of 0.180-0.250 mm, 0.250-0.425 mm, and 0.425-0.850 mm. Each sample was used in a temperature ramp test (light-off test) from room temperature to 500 °C, applying a heating rate of 5 °C min⁻¹.

External diffusion limitations were evaluated through three temperature ramp tests (light-off tests) from room temperature to 500 °C, with a heating rate of 5 °C min<sup>-1</sup>, using a catalyst with particle size between 0.250 mm and 0.425 mm. The space velocity was 30 m³ kg<sup>-1</sup> h<sup>-1</sup> in the three tests, but different volumetric flow rates and catalyst masses were used in each test. In the first test, the volumetric flow rate was 25 mL min<sup>-1</sup> and the mass 50 mg; in the second test, the volumetric flow rate was 35 mL min<sup>-1</sup> and the mass 70 mg; in the third test, the volumetric flow rate was 45 mL min<sup>-1</sup> and the mass 90 mg.

#### 2.3.3 Stability test

In the RWGS reaction, copper catalysts can deactivate mainly due to sintering and reoxidation (Bahmanpour *et al.*, 2019). Thus, a long-term test was performed to analyze the stability of the catalyst. After pretreatment, the sample was heated at a rate of 5 °C min<sup>-1</sup> until 500 °C, maintaining this temperature for more than 9 hours under the flow of mixture 1 (H<sub>2</sub>/CO<sub>2</sub> molar ratio of 1) at 18 m<sup>3</sup> kg<sup>-1</sup> h<sup>-1</sup>.

## 2.3.4 Catalytic tests at fixed temperatures

Aiming at evaluating the CO<sub>2</sub> conversion in the RWGS reaction, avoiding interferences arising from the dynamics of the catalytic system (that may occur on the same time scale as the heating rate), catalytic tests were also performed at fixed temperatures. In such experiments, CO<sub>2</sub> conversion data were obtained after the catalyst activity reached a steady state. Three temperature levels were applied: 330 °C, 380 °C, and 430 °C. In order to achieve these temperatures, the samples were subjected to a heating rate of 5 °C min<sup>-1</sup> after the pretreatment. CO<sub>2</sub> conversion was also investigated under different space velocities and inlet composition conditions. The space velocities applied were 18 m³ kg<sup>-1</sup> h<sup>-1</sup>, 30 m³ kg<sup>-1</sup> h<sup>-1</sup> and 42 m³ kg<sup>-1</sup> h<sup>-1</sup>, and the feed composition effect was observed performing the tests at fixed

temperatures with mixture 1 ( $H_2/CO_2$  molar ratio of 1), mixture 2 ( $H_2/CO_2$  molar ratio of 2.5) and mixture 3 ( $H_2/CO_2$  molar ratio of 4).

In each condition, the catalyst was exposed to the reaction mixture until stable conversion was achieved.

The objective of these experiments is to check if the curves obtained at temperature ramp tests can provide results equivalent to conventional catalytic tests.

## 2.4 Kinetic modeling

Among the different kinetic studies available in the literature involving the RWGS reaction, three were chosen to be studied, based on the type of catalyst and reactor used. The first model investigated was proposed by Ginés, Marchi and Apesteguía (1997):

$$r_{RWGS} = \frac{k_1 L_0 \left( P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1} \right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_8^* K_{24}^*} \cdot P_{CO}}$$
(25)

Since the authors do not specify an expression for determining the equilibrium constant  $K_1$ , it was calculated through the equation (28), the same expression used in the other two models studied in the present work.

$$K_1 = 10^{\left(-\frac{2073}{T} + 2.029\right)} \tag{28}$$

It is possible to observe that, in reaction (25), there is a set of parameters to adjust in order to determine the reaction rate.  $k_1$  and  $k_2$  were taken as a single parameter, to be fitted together with  $k_3$  and  $k_2$ .

However, the parameters by Ginés, Marchi, and Apesteguía (1997) are temperature-dependent, so each temperature has its own set of associated parameters. Intending to obtain temperature-independent parameters, the present work took the initiative of adapting the parameters  $k_1L_0$ ,  $K_8^*$ , and  $K_{24}^*$ , considering a

temperature dependence pattern described by the Arrhenius expression, so that  $k_1L_0$  becomes:

$$k_1 \cdot L_0 = k_{1,0} \cdot L_0 \cdot e^{-\frac{E_{a,1}}{R \cdot T}} \tag{43}$$

in which  $k_{1,0}$  is the pre-exponential factor in atm<sup>-1</sup> h<sup>-1</sup>,  $E_{a,1}$  is the apparent activation energy in kcal mol<sup>-1</sup>, R is the universal gas constant in kcal K<sup>-1</sup> mol<sup>-1</sup>, and T is the temperature in K.

It was also assumed that a rate constant  $k_2$  governs the forward reaction (8), while in the reverse direction, the constant is  $k_{-2}$ . Similarly, the forward reaction (24) has  $k_3$  as the rate constant, and the reverse reaction has a rate constant  $k_{-3}$ . Therefore, the equilibrium constants  $K_8^*$  and the product of constants  $K_8^*$  can be written as:

$$K_8^* = \frac{k_2}{k_{-2}} \tag{44}$$

$$K_8^* \cdot K_{24}^* = \frac{k_2}{k_{-2}} \cdot \frac{k_3}{k_{-3}} \tag{45}$$

Nevertheless, these rate constants can be expressed in terms of the Arrhenius expression as well:

$$K_8^* = \frac{k_{2,0} \cdot e^{-\frac{E_{a,2}}{R \cdot T}}}{k_{-2,0} \cdot e^{-\frac{E_{a,-2}}{R \cdot T}}}$$
(46)

$$K_8^* \cdot K_{24}^* = \frac{k_{2,0} \cdot e^{-\frac{E_{a,2}}{R \cdot T}}}{k_{-2,0} \cdot e^{-\frac{E_{a,-2}}{R \cdot T}}} \cdot \frac{k_{3,0} \cdot e^{-\frac{E_{a,3}}{R \cdot T}}}{k_{-3,0} \cdot e^{-\frac{E_{a,-3}}{R \cdot T}}}$$
(47)

where  $k_{2,0}$  represents the pre-exponential factor of forward reaction (8),  $k_{-2,0}$  is the pre-exponential factor of reverse reaction (8),  $E_{a,2}$  is the apparent activation energy of the forward reaction (8),  $E_{a,-2}$  is the apparent activation energy of reverse reaction (8),  $k_{3,0}$  represents the pre-exponential factor of forward reaction (24),  $k_{-3,0}$  is the pre-exponential factor of reverse reaction (24),  $E_{a,3}$  is the apparent activation energy of

the forward reaction (24) and  $E_{a,-3}$  is the apparent activation energy of reverse reaction (24). Therefore, equations (46) and (47) can be written as:

$$K_8^* = \frac{k_{2,0}}{k_{-2,0}} \cdot e^{-\left(\frac{E_{a,2}}{R \cdot T} - \frac{E_{a,-2}}{R \cdot T}\right)} \tag{48}$$

$$K_8^* \cdot K_{24}^* = \frac{k_{2,0}}{k_{-2,0}} \cdot e^{-\left(\frac{E_{a,2}}{R \cdot T} - \frac{E_{a,-2}}{R \cdot T}\right)} \cdot \frac{k_{3,0}}{k_{-3,0}} \cdot e^{-\left(\frac{E_{a,3}}{R \cdot T} - \frac{E_{a,-3}}{R \cdot T}\right)}$$
(49)

Giving rise to:

$$K_8^* = \frac{k_{2,0}}{k_{-2,0}} \cdot e^{-\frac{(E_{a,2} - E_{a,-2})}{RT}}$$
 (50)

$$K_8^* \cdot K_{24}^* = \frac{k_{2,0}}{k_{-2,0}} \cdot e^{-\frac{(E_{a,2} - E_{a,-2})}{RT}} \cdot \frac{k_{3,0}}{k_{-3,0}} \cdot e^{-\frac{(E_{a,3} - E_{a,-3})}{RT}}$$
(51)

Defining parameters  $k_{4,0}$  in atm<sup>-1</sup>,  $k_{5,0}$  (dimensionless), and the activation energy differences  $\Delta E_{a,4}$  and  $\Delta E_{a,5}$ , both in kcal mol<sup>-1</sup>:

$$k_{4,0} = \frac{k_{2,0}}{k_{-2,0}} \tag{52}$$

$$k_{5,0} = \frac{k_{2,0} \cdot k_{3,0}}{k_{-2,0} \cdot k_{-3,0}} \tag{53}$$

$$\Delta E_{a,4} = E_{a,2} - E_{a,-2} \tag{54}$$

$$\Delta E_{a,5} = (E_{a,2} + E_{a,3}) - (E_{a,-2} + E_{a,-3})$$
(55)

At last, the equilibrium constants turn into:

$$K_8^* = k_{4.0} \cdot e^{-\left(\frac{\Delta E_{a,4}}{R \cdot T}\right)}$$
 (56)

$$K_8^* \cdot K_{24}^* = k_{5,0} \cdot e^{-\left(\frac{\Delta E_{a,5}}{R \cdot T}\right)}$$
 (57)

Accordingly, the modeling of a RWGS reactor through the rate equation proposed by Ginés, Marchi and Apesteguía requires the fitting of six parameters:  $k_{1,0}$ ,  $E_{a,1}$ ,  $k_{4,0}$ ,  $\Delta E_{a,4}$ ,  $k_{5,0}$  and  $\Delta E_{a,5}$ .

The second model studied was the model of Vanden Bussche and Froment (1996), given by equation (26). A new fitting based on the same parameters presented by the authors was conducted.

$$r_{RWGS} = \frac{k_1 \cdot P_{CO_2} \cdot \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{P_{H_2O} \cdot P_{CO}}{P_{CO_2} \cdot P_{H_2}}\right)\right)}{\left(1 + \left(\frac{K_{H_2O}}{K_{15}^* K_{16}^* K_{H_2}}\right) \left(\frac{P_{H_2O}}{P_{H_2}}\right) + \sqrt{K_{H_2} \cdot P_{H_2}} + K_{H_2O} \cdot P_{H_2O}\right)}$$
(26)

The third model studied was the model of Graaf, Stamhuis and Beenackers (1988), also adjusting the parameters originally proposed by the authors.

$$r_{RWGS} = \frac{k_1 \cdot K_{CO_2} \cdot \left( f_{CO_2} \cdot f_{H_2} - \frac{f_{H_2O} \cdot f_{CO}}{K_1} \right)}{\left( 1 + K_{CO} \cdot f_{CO} + K_{CO_2} \cdot f_{CO_2} \right) \left( f_{H_2}^{0.5} + f_{H_2O} \cdot \left( \frac{K_{H_2O}}{K_{H_2}^{0.5}} \right) \right)}$$
(39)

#### 2.5 Reactor modeling

A one-dimensional pseudo-homogeneous fixed bed reactor model was developed to provide  $CO_2$  conversion as a function of the mass of the catalyst in contact with the fluid flowing through the bed. This system has the catalyst mass, W in kg, as an independent variable. The dependent variables, in turn, are the molar flow rates of each component,  $F_{CO_2}$ ,  $F_{H_2}$ ,  $F_{CO}$ ,  $F_{H_{2O}}$  and  $F_{He}$ , which can be expressed by  $F_i$  in mol s<sup>-1</sup>. The following simplifying assumptions were assumed:

- a) Uniform and constant cross-sectional area;
- b) Isothermal system;
- c) Unidirectional flow;
- d) Uniform flow at the catalyst inlet;
- e) No diffusion limitations;
- f) Ideal gas behavior;
- g) Steady-state;

- h) Uniform axial velocity;
- i) Isobaric system.

Neither energy balance nor momentum balance were considered, as a result of hypotheses (b), (c), (h) and (i). A differential material balance was carried out according to:

$$\{input\} - \{output\} + \{generation\} = \{accumulation\}$$
 (58)

The input term, in this case, is given by  $F_i|_W$ , which is the molar flow rate of component i at a given mass of catalyst W along the bed, while the output term is expressed by  $F_i|_{W+dW}$ , which consists of the molar flow rate of component i after the reaction mixture has already passed through a corresponding mass of catalyst to W+dW. The accumulation term is equal to zero, as a consequence of having assumed hypothesis (g). The generation term is given by  $R_i$  dW and is expressed by equation (59):

$$R_i = \nu_i \cdot r_{RWGS} \tag{59}$$

where  $R_i$  indicates the generation or consumption rate of component i in mol s<sup>-1</sup> kg<sup>-1</sup>,  $v_i$  is the stoichiometric coefficient of component i in the RWGS reaction (dimensionless, negative for reactants and positive for products), and  $r_{RWGS}$  represents the rate of RWGS reaction in mol s<sup>-1</sup> kg<sup>-1</sup>.

Therefore, the complete material balance is given by:

$$0 = F_i|_W - F_i|_{W+dW} + R_i \cdot dW {(60)}$$

Dividing both sides of the equation by *dW*:

$$0 = \frac{F_i|_W - F_i|_{W+dW}}{dW} + R_i \tag{61}$$

Let  $dW \rightarrow 0$ , then:

$$0 = \frac{-dF_i}{dW} + R_i \tag{62}$$

Therefore, the material balance for each component is given by:

$$\frac{dF_{CO_2}}{dW} = -r_{RWGS} \tag{63}$$

$$\frac{dF_{H_2}}{dW} = -r_{RWGS} \tag{64}$$

$$\frac{dF_{CO}}{dW} = r_{RWGS} \tag{65}$$

$$\frac{dF_{H_2O}}{dW} = r_{RWGS} \tag{66}$$

$$\frac{dF_{He}}{dW} = 0 ag{67}$$

After that, the rate equations were introduced into the balance and a dimensionless version of each set of equations was proposed (the details of the derivation of each model are shown in Appendix A), as follows:

Model of Ginés, Marchi and Apesteguía (1997):

$$\frac{dy_{CO_2}}{dm} = -\frac{A \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{CO}^2}{K_1}\right)}{y_{H_2} + B \cdot y_{H_2}^{1.5} + D \cdot y_{CO}}$$
(68)

$$\frac{dy_{H_2}}{dm} = -\frac{A \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{CO}^2}{K_1}\right)}{y_{H_2} + B \cdot y_{H_2}^{1.5} + D \cdot y_{CO}}$$
(69)

$$\frac{dy_{co}}{dm} = \frac{A \cdot \left(y_{co_2} \cdot y_{H_2} - \frac{y_{co}^2}{K_1}\right)}{y_{H_2} + B \cdot y_{H_2}^{1.5} + D \cdot y_{co}}$$
(70)

$$\frac{dy_{H_2O}}{dm} = \frac{A \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{CO}^2}{K_1}\right)}{y_{H_2} + B \cdot y_{H_2}^{1.5} + D \cdot y_{CO}}$$
(71)

$$\frac{dy_{He}}{dm} = 0 ag{72}$$

Model of Vanden Bussche and Froment (1996):

$$\frac{dy_{CO_2}}{dm} = -\frac{E \cdot y_{CO_2} \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{y_{H_2O} \cdot y_{CO}}{y_{CO_2} \cdot y_{H_2}}\right)\right)}{\left(1 + G\left(\frac{y_{H_2O}}{y_{H_2}}\right) + H \cdot \sqrt{y_{H_2}} + I \cdot y_{H_2O}\right)}$$
(73)

$$\frac{dy_{H_2}}{dm} = -\frac{E \cdot y_{CO_2} \left( 1 - \left( \frac{1}{K_1} \right) \cdot \left( \frac{y_{H_2O} \cdot y_{CO}}{y_{CO_2} \cdot y_{H_2}} \right) \right)}{\left( 1 + G \left( \frac{y_{H_2O}}{y_{H_2}} \right) + H \cdot \sqrt{y_{H_2}} + I \cdot y_{H_2O} \right)}$$
(74)

$$\frac{dy_{CO}}{dm} = \frac{E \cdot y_{CO_2} \left( 1 - \left( \frac{1}{K_1} \right) \cdot \left( \frac{y_{H_2O} \cdot y_{CO}}{y_{CO_2} \cdot y_{H_2}} \right) \right)}{\left( 1 + G \left( \frac{y_{H_2O}}{y_{H_2}} \right) + H \cdot \sqrt{y_{H_2}} + I \cdot y_{H_2O} \right)}$$
(75)

$$\frac{dy_{H_2O}}{dm} = \frac{E \cdot y_{CO_2} \left( 1 - \left( \frac{1}{K_1} \right) \cdot \left( \frac{y_{H_2O} \cdot y_{CO}}{y_{CO_2} \cdot y_{H_2}} \right) \right)}{\left( 1 + G \left( \frac{y_{H_2O}}{y_{H_2}} \right) + H \cdot \sqrt{y_{H_2}} + I \cdot y_{H_2O} \right)}$$
(76)

$$\frac{dy_{He}}{dm} = 0 ag{77}$$

Model of Graaf, Stamhuis and Beenackers (1988):

$$\frac{dy_{CO_2}}{dm} = -\frac{J \cdot N \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{H_2O} \cdot y_{CO}}{K_1}\right)}{\left(1 + L \cdot y_{CO} + N \cdot y_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(78)

$$\frac{dy_{H_2}}{dm} = -\frac{J \cdot N \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{H_2O} \cdot y_{CO}}{K_1}\right)}{\left(1 + L \cdot y_{CO} + N \cdot y_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(79)

$$\frac{dy_{CO}}{dm} = \frac{J \cdot N \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{H_2O} \cdot y_{CO}}{K_1}\right)}{\left(1 + L \cdot y_{CO} + N \cdot y_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(80)

$$\frac{dy_{H_2O}}{dm} = \frac{J \cdot N \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{H_2O} \cdot y_{CO}}{K_1}\right)}{\left(1 + L \cdot y_{CO} + N \cdot y_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(81)

$$\frac{dy_{He}}{dm} = 0 ag{82}$$

Dimensionless variables:

*m* is the dimensionless mass, given by:

$$m = \frac{W}{W_0} \tag{83}$$

where  $W_0$  is the total catalyst mass.

 $y_i$  is the molar fraction of the component i:

$$y_i = \frac{P_i}{P} \tag{84}$$

where  $P_i$  is the partial pressure of the component i, and P is the total pressure.

Dimensionless model parameters:

$$A = \frac{k_1 L_0 \cdot R \cdot T \cdot W_0}{q} \tag{85}$$

$$B = \sqrt{K_8^* \cdot P} \tag{86}$$

$$D = \frac{1}{K_8^* K_{24}^*} \tag{87}$$

$$E = \frac{k_1 \cdot R \cdot T \cdot f_P \cdot W_0}{q} \tag{88}$$

$$G = \frac{K_{H_2O}}{K_{15}^* K_{16}^* K_{H_2}} \tag{89}$$

$$H = \sqrt{K_{H_2} \cdot P} \tag{90}$$

$$I = K_{H_2O} \cdot P \tag{91}$$

$$J = \frac{k_1 \cdot R \cdot T \cdot f_P \cdot W_0 \cdot \sqrt{P}}{q \cdot P} \tag{92}$$

$$L = K_{CO} \cdot P \tag{93}$$

$$N = K_{CO_2} \cdot P \tag{94}$$

$$Q = \frac{K_{H_2O} \cdot \sqrt{P}}{K_{H_2}^{0.5}} \tag{95}$$

in which q is the volumetric flow rate, and  $f_P$  is a correction factor for pressure, with value of  $10^{-5}$  bar Pa<sup>-1</sup>.

#### 2.6 Reactor simulation and kinetic parameter estimation

The reactor model was implemented through a computational routine in Python language. The conservation equations were integrated using the LSODA solver through the odeint package in the SciPy module. The integration was carried out for 1000 points between m = 0 and m = 1, with the following initial conditions:

$$y_{CO_2}\big|_{m=0} = 0.1 \tag{96}$$

$$y_{H_2}\big|_{m=0} = y_{H_2}^0 \tag{97}$$

$$y_{CO}|_{m=0} = 0 (98)$$

$$y_{H_2O}\big|_{m=0} = 0 (99)$$

$$y_{He}|_{m=0} = 1 - \left[0.1 + \left(y_{H_2}|_{m=0}\right)\right]$$
 (100)

where  $y_{H2}^{0}$  is the molar fraction of H<sub>2</sub> in the feed (0.10 for mixture 1, 0.25 for mixture 2 and 0.40 for mixture 3).

The determination of the kinetic parameters was conducted through a parameter estimation procedure based on an optimization problem solved with the Scipy module through the Differential Evolution method, presented by Storn and Price (1997), which, for each model, returned the respective set of parameters capable of minimizing the following objective function:

$$f_{obj} = \sum_{d} (X_{CALC_d} - X_{EXP_d})^2$$
 (101)

where d is the pool of all the different sets of operational conditions, composed by temperature, space velocity and  $H_2/CO_2$  molar ratio,  $X_{CALC,d}$  is the  $CO_2$  conversion predicted by the model for certain operational conditions, and  $X_{EXP,d}$  is the experimental  $CO_2$  conversion obtained under the same conditions. The  $CO_2$  conversion is given by:

$$X = \frac{y_{CO_2}^0 - y_{CO_2}}{y_{CO_2}^0} \tag{102}$$

being X the  $CO_2$  conversion and  $y^0_{CO2}$  is the molar fraction of  $CO_2$  in the feed. The upper and lower limits used in the search for the global optimum were within the order of magnitude of the respective parameters described in the literature for each model.

#### **3 RESULTS AND DISCUSSIONS**

# 3.1 Catalyst characterization

The commercial CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst used in the present work has a mass composition of 71% CuO, 24% ZnO and 5% Al<sub>2</sub>O<sub>3</sub>, as determined in previous research by our team (Gonzalez, 2017). In Figure 1, which shows the X-ray diffractogram of the calcined CuO/ZnO/Al<sub>2</sub>O<sub>3</sub>, the presence of CuO and ZnO is confirmed by the occurrence of their characteristic diffraction peaks. A diffraction peak characteristic of graphite also appears, probably due to the addition of 1.5% by mass of additive during the tableting of the catalyst (Gonzalez, 2017; Chu *et al.*, 2013). The non-detection of alumina by X-ray diffraction is probably because its presence occurs in the amorphous phase.

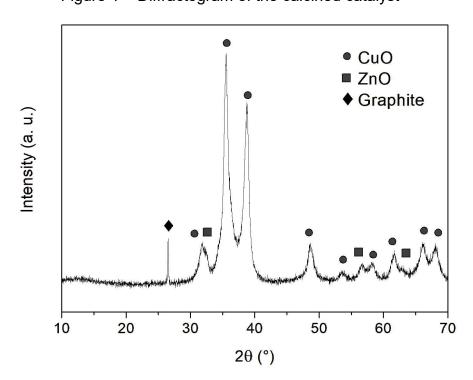


Figure 1 – Diffractogram of the calcined catalyst

The results of the TPR test are presented in Figure 2, in which a peak close to 207 °C can be observed. This maximum represents the reduction of CuO to metallic copper. Table 1 provides a comparison between the experimental H<sub>2</sub> consumption and the theoretical value, determined by the catalyst composition.

(i) (i) (ii) (iii) (iii)

Figure 2 – TPR profile of the calcined catalyst

Source: The author, 2024.

Table 1 – Experimental and theoretical consumption of H<sub>2</sub>

Experimental H <sub>2</sub>	Theoretical H <sub>2</sub>	Ratio between experimental
consumption	consumption	and theoretical H <sub>2</sub>
(mmol g <sub>cat</sub> <sup>-1</sup> )	(mmol g <sub>cat</sub> -1)	consumption (%)
8.647	8.926	97

Source: The author, 2024.

The theoretical consumption of  $H_2$  was calculated considering a molar mass of 79.545 g/mol for CuO and a stoichiometric ratio of 1:1 between CuO and  $H_2$  in the reduction of copper oxide, according to the equation (103).

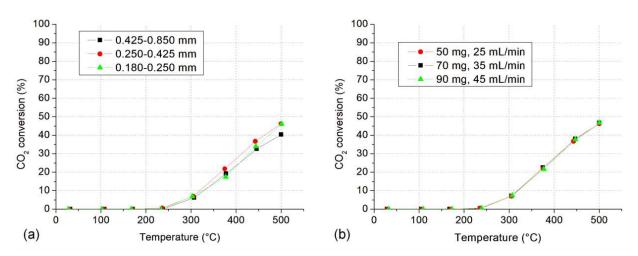
$$\frac{1 \, mol \, H_2}{1 \, mol \, CuO} \cdot \frac{1 \, mol \, CuO}{79.545 \, g} \cdot \frac{71 \, g}{100 \, g \, sample} = \frac{8.926 \cdot 10^{-3} \, mol \, H_2}{g \, sample}$$
(103)

From the ratio between the experimental H<sub>2</sub> consumption and the theoretical value, it is possible to conclude that practically all copper oxide was reduced to metallic copper (Gonzalez, 2017; Blanco *et al.*, 2019; Dasireddy *et al.*, 2018).

#### 3.2 Analysis of diffusional effects

Figure 3 presents the results of the evaluation of possible diffusional effects. The outcomes obtained under the different conditions were quite close, within a tolerance range, concluding that it was possible to disregard internal and external diffusional limitations under the conditions used in the tests of the present work. This means the system is under chemical kinetic control (Zhang *et al.*, 2019). Thus, the applicability of hypothesis (e) (no diffusion limitations) to the modeling of the reactor was confirmed.

Figure 3 – CO<sub>2</sub> conversion versus temperature during the experiments for evaluation of diffusional limitations, at 30 m³ kg<sup>-1</sup> h<sup>-1</sup>, with H<sub>2</sub>:CO<sub>2</sub> molar ratio of 4:1

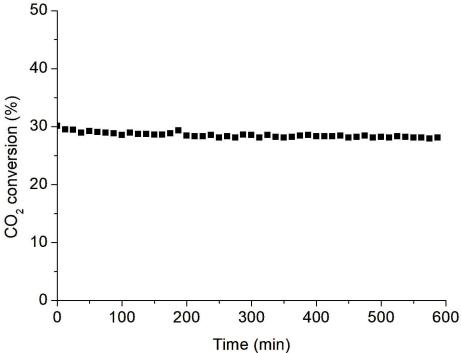


Legend: (a) – Evaluation of internal diffusional effects; (b) – Evaluation of external diffusional effects, with particle size range between 0.250 mm and 0.425 mm.

## 3.3 Stability evaluation

Figure 4 presents the results of the stability evaluation. It is possible to observe that the commercial catalyst presented consistent performance, maintaining CO<sub>2</sub> conversion at around 28% for more than nine hours. Therefore, this indicates no meaningful catalyst deactivation under the test conditions. No significant methane formation was detected.

Figure 4 –  $CO_2$  conversion versus time during the stability test at 500 °C, 18 m³ kg<sup>-1</sup> h<sup>-1</sup> and H<sub>2</sub>: $CO_2$  = 1:1



Source: The author, 2024.

In the same way, carbon monoxide was the only carbon-containing compound produced in all the light-off and fixed-temperature tests carried out in this work, pointing out that the catalyst performs 100% selectivity to CO.

## 3.4 Thermodynamic modeling

The equation (28) by Graaf *et al.* (1986) allows the calculation of the chemical equilibrium constant of the RWGS equation and, therefore, of the equilibrium CO<sub>2</sub> conversion as a function of temperature.

$$K_1 = 10^{\left(-\frac{2073}{T} + 2.029\right)} \tag{28}$$

The same equation was applied to calculate the equilibrium conversion through a computational routine in Python language, using the fsolve solver from the optimize library in the SciPy module. The mathematical procedure adopted is detailed in Appendix B.

Figure 5 shows the variation of  $K_1$  as a function of temperature, confirming the expected trend for the constant to increase with increasing temperature due to the endothermicity of the reaction.

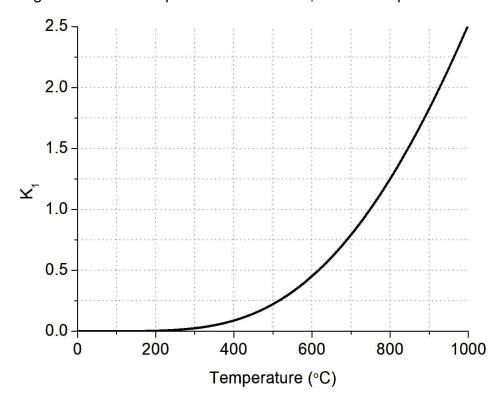


Figure 5 – RWGS equilibrium constant K<sub>1</sub> versus temperature

Figure 6 presents the simulation results of carbon dioxide conversion at equilibrium as a function of temperature for the three  $H_2/CO_2$  molar ratios studied. The thermodynamic curve points to two main trends: the increase in equilibrium conversion with increasing temperature, motivated by the rise in the  $K_1$  constant, and, for the same temperature, a higher equilibrium conversion for higher  $H_2/CO_2$  ratios, due to the presence of more reagent in the medium shifting the equilibrium towards  $CO_2$  conversion.

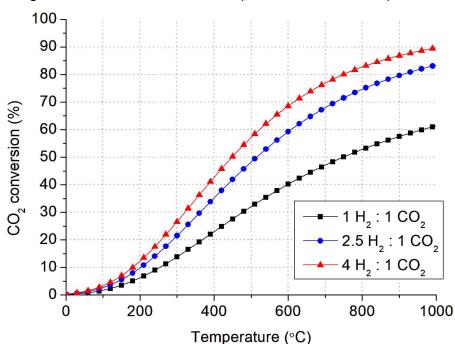


Figure 6 – CO<sub>2</sub> conversion at equilibrium versus temperature

Source: The author, 2024.

If Gibbs free energy ( $\Delta G_R$ ) of the reaction is negative, RWGS tends to occur spontaneously. If, however,  $\Delta G_R$  is greater than zero, the forward WGS reaction tends to occur. At constant temperature and pressure,  $\Delta G_R$  is expressed by (Atkins; Jones, 2006):

$$\Delta G_R = \Delta G_R^{\circ} + RT \cdot \ln Q_1 \tag{104}$$

where  $\Delta G^{\circ}_{R}$  is the Standard Gibbs Free Energy of reaction, R is the universal gas constant, T is the temperature and  $Q_{1}$  is given by (Atkins; Jones, 2006):

$$Q_1 = \frac{P_{CO} \cdot P_{H_2O}}{P_{CO_2} \cdot P_{H_2}} \tag{105}$$

At equilibrium, the equilibrium constant  $K_1$  is equal to  $Q_1$  and  $\Delta G_R = 0$ , thus equation (104) turns into (Atkins; Jones, 2006):

$$\Delta G^{\circ}_{R} = -RT \cdot \ln K_{1} \tag{106}$$

Otherwise, using a feed mixture with a  $H_2/CO_2$  molar ratio greater than 1 means working with a reaction quotient  $Q_1$  lower than  $K_1$ , because the reactants are in the denominator of  $Q_1$ . Therefore, the reaction will proceed in the direction of the formation of CO and  $H_2O$ , so that  $Q_1$  increases until it equals  $K_1$ . The higher the  $H_2/CO_2$  ratio, the lower the value of  $Q_1$  and the more the equilibrium will be shifted towards the consumption of  $CO_2$ . This helps to understand that the conversions achieved were higher with larger excesses of  $H_2$  (Atkins; Jones, 2006).

The effect of the temperature in the equilibrium can be explained through Le Châtelier Principle, expressed through van't Hoff equation, (107) (Atkins; Jones, 2006):

$$\ln \frac{K_2}{K_1} = \frac{\Delta H^{\circ}_R}{R} \cdot \left(\frac{1}{T_1} - \frac{1}{T_2}\right) \tag{107}$$

where  $K_2$  is the equilibrium constant at temperature  $T_2$ ,  $K_1$  is the equilibrium constant at temperature  $T_1$  and  $\Delta H^{\circ}_R$  is the standard enthalpy of reaction. RWGS reaction is endothermic, then  $\Delta H^{\circ}_R > 0$ . If  $T_2$  is higher than  $T_1$ ,  $1/T_2$  will be smaller than  $1/T_1$ , thereby the term between parenthesis will be positive. Therefore,  $\ln(K_2/K_1)$  is necessarily positive, which means the constant  $K_2$  is greater than  $K_1$ . Thus, using a higher temperature favors  $CO_2$  and  $CO_2$  and  $CO_3$  and  $CO_4$  and  $CO_4$  formation (Atkins; Jones, 2006).

# 3.5 Effects of composition, space velocity, and temperature in catalytic tests conducted at a fixed temperature

Figures 7, 8 and 9 show the results of the tests at a fixed temperature. The conversion data presented are the average CO<sub>2</sub> conversion values recorded after reaching a steady state, gathered in Appendix C. To better guide the discussion, each graph shows the CO<sub>2</sub> conversion at a given constant operating condition (space velocity, temperature, H<sub>2</sub>:CO<sub>2</sub> ratio in the feed), showing the different outcomes obtained with the variation of the other two conditions.

#### 3.5.1 Effect of the feed composition

Figure 7 illustrates the direct relation that the H<sub>2</sub>:CO<sub>2</sub> molar ratio in the feed has with CO<sub>2</sub> conversion, for the same space velocity. The results at 430 °C were chosen because they provide a clearer view, but at 330 °C and 380 °C the effect is equivalent.

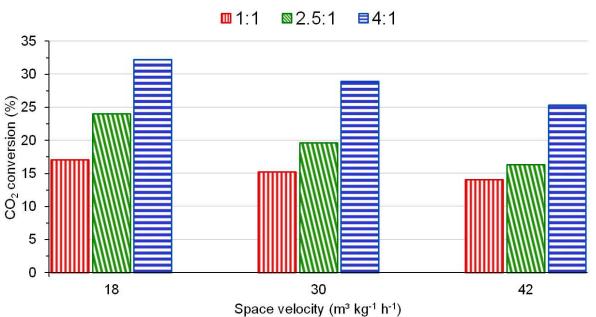


Figure 7 – Experimental results of CO<sub>2</sub> conversion at 430 °C for different H<sub>2</sub>:CO<sub>2</sub> molar ratios at the three space velocities

From a kinetic point of view, higher H<sub>2</sub> partial pressures may be associated with a higher hydrogen coverage and a higher adsorption capacity on the catalyst surface. In H<sub>2</sub>-poor reaction mixtures, preferential adsorption of CO<sub>2</sub> may lead to a CO<sub>2</sub>-rich surface, reducing the chances of the reactants interacting. This is mitigated when higher H<sub>2</sub> partial pressures are used (Reina; Odriozola; Arellano-Garcia, 2021). Ginés, Marchi, and Apesteguía (1997) studied the effect of the inlet composition on the initial reaction rate with CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalysts, changing the H<sub>2</sub>/CO<sub>2</sub> molar ratio between 0.3 and 9.0. They stated that a reconstruction of the copper surface takes place at ratios of 3 or over, making the surface more reactive to dissociative CO<sub>2</sub> adsorption.

## 3.5.2 Effect of the space velocity

The effect of the space velocity can be observed in Figure 8. The results with mixture 3 (H<sub>2</sub>:CO<sub>2</sub> molar ratio of 4:1) were chosen because they provide a clearer view, but with mixtures 1 and 2 the effect is equivalent.

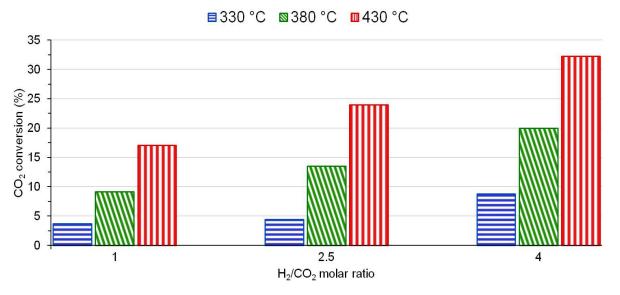
Figure 8 – Experimental results of CO<sub>2</sub> conversion with 4 H<sub>2</sub>:1 CO<sub>2</sub> molar ratio for different space velocities at the three temperatures

Lower space velocities lead to higher CO<sub>2</sub> conversions, for the same temperature. For each of the temperature levels studied, the conversion at 18 m³ kg<sup>-1</sup> h<sup>-1</sup> is always higher than that at 30 m³ kg<sup>-1</sup> h<sup>-1</sup>, which, in turn, is higher than the conversion at 42 m³ kg<sup>-1</sup> h<sup>-1</sup>. This effect is related to the fact that a higher spatial velocity causes the residence time to be shorter. Therefore, the contact time provided between the reactants and the catalytic surface is shorter, leading to a decrease in conversion (Park *et al.*, 2014; Ojeda, 2022).

# 3.5.3 Effect of the temperature

In Figure 9, is possible to observe the influence of temperature on RWGS reaction for the same space velocity. The results at 18 m³ kg⁻¹ h⁻¹ were chosen because they provide a clearer view, but at 30 m³ kg⁻¹ h⁻¹ and 42 m³ kg⁻¹ h⁻¹ the effect is equivalent.

Figure 9 – Experimental results of CO<sub>2</sub> conversion at 18 m<sup>3</sup> kg<sup>-1</sup> h<sup>-1</sup> for different temperatures at the three H<sub>2</sub>/CO<sub>2</sub> molar ratios



The difference in temperature affects the kinetic constant, as shown by the Arrhenius equation:

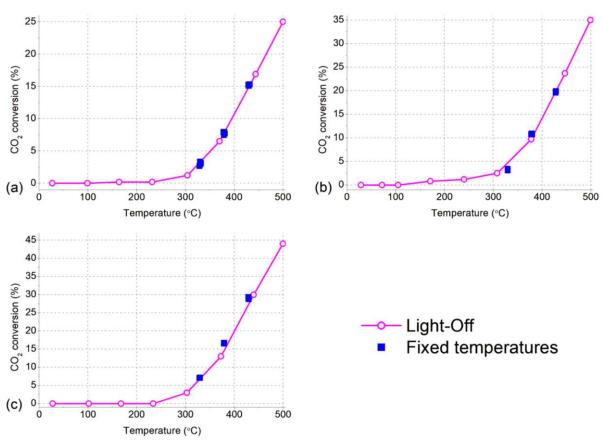
$$\ln k_1 = \ln k_{1,0} - \frac{E_{a,1}}{R \cdot T} \tag{108}$$

As can be seen in equation (108), the higher the value of T, the lower the magnitude of the negative term. As a result, the value of  $ln(k_1)$  will be higher, thus  $k_1$  will be larger as well, leading to a higher rate constant and, consequently, a higher reaction rate.

# 3.6 Comparison between light-off tests and fixed temperature tests

Figure 10 presents the results of the light-off tests carried out at 30 m³ kg $^{-1}$  h $^{-1}$  with H $_2$ /CO $_2$  molar ratios of 1:1, 2.5:1, and 4:1. The conversion and temperature data obtained from these tests are listed in Appendix D. The same graph also shows the CO $_2$  conversion obtained through the catalytic runs at fixed temperatures with the three molar ratios studied at 30 m³ kg $^{-1}$  h $^{-1}$ . The highest conversion is obtained with the molar ratio 4 H $_2$ :1 CO $_2$ , while the lowest conversion at the same temperature is associated with the reaction mixture with a molar ratio of 1:1. As expected, Mixture 2, with an intermediate H $_2$ /CO $_2$  ratio, provided intermediate conversion values.

Figure 10 – Experimental results of  $CO_2$  conversion vs. temperature at 30 m<sup>3</sup>  $kg^{-1}$  h<sup>-1</sup> with different  $H_2/CO_2$  molar ratios in light-off tests and fixed-temperature tests



Legend: (a)  $-H_2/CO_2$  molar ratio of 1:1; (b)  $-H_2/CO_2$  molar ratio of 2.5:1; (c)  $-H_2/CO_2$  molar ratio of 4:1.

Source: The author, 2024.

It is also possible to identify in Figure 10 a significant consistency between the values obtained by light-off tests and tests at fixed temperatures. This indicates that, on the commercial CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst, there is no significant influence of possible transient processes in CO<sub>2</sub> conversion along the temperature ramp under the conditions defined for the experiments. Therefore, obtaining kinetic parameters from data provided by light-off curves turns out to be a concrete possibility that will be applied in the following sections.

## 3.7 Light-off curves simulation with kinetic parameters from the literature

The simulation of the light-off curves was conducted using the values of the kinetic parameters originally reported in the literature. Because one of the parameters of the Ginés, Marchi, and Apesteguía (1997) model was not reported in the original paper, it was not possible to simulate the light-off curve using this model.

Vanden Bussche and Froment (1996) carried out 276 experiments, varying the temperature between 180 and 280 °C, the CO/CO<sub>2</sub> ratio between 0 and 4.1, and the total pressure between 15 and 51 bar to produce the kinetic data used to fit the parameters of their kinetic model for methanol synthesis on a commercial CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst. The values of the parameters reported in the original paper are listed in Table 2.

Table 2 – Kinetic parameters obtained by Vanden Bussche and Froment (1996)

Parameter	Value	
A <sub>√KH2</sub> (bar <sup>-0,5</sup> )	0.499	
$B_{\lor KH2}$ (J mol <sup>-1</sup> )	17197	
<i>A<sub>KH2O</sub></i> (bar <sup>-1</sup> )	6.62·10 <sup>-11</sup>	
$B_{KH2O}$ (J mol <sup>-1</sup> )	124119	
A <sub>KH2O/K15*K16*KH2</sub>	3453.38	
A <sub>k1</sub> (mol kg <sup>-1</sup> s <sup>-1</sup> bar <sup>-1</sup> )	1.22·10 <sup>10</sup>	
$B_{k1}$ (J mol <sup>-1</sup> )	-94765	

Source: Vanden Bussche; Froment, 1996.

In their kinetic study of low-pressure methanol synthesis over a commercial Cu–Zn–Al catalyst, Graaf, Stamhuis, and Beenackers (1988) carried out a series of experiments under steady-state conditions. Temperatures between 210.4 °C and 243.6 °C were applied, at total pressures of 15 bar, 30 bar and 50 bar, space velocities between 0.1 m³ s⁻¹ kg⁻¹ and 7 m³ s⁻¹ kg⁻¹, CO/CO₂ molar ratios between 0 and 5.7 in the feed, and H₂/CO₂ molar ratios between 2.6 and 40.9 in the feed. They obtained the parameters shown in Table 3.

Table 3 – Kinetic parameters obtained by Graaf, Stamhuis and Beenackers (1988)

Parameter	Value
A <sub>k1</sub> (mol s <sup>-1</sup> kg <sup>-1</sup> bar <sup>-0.5</sup> )	$(7.31 \pm 4.90) \cdot 10^8$
$B_{k1}$ (J mol <sup>-1</sup> )	-123400 ± 1600
A <sub>KCO</sub> (bar)	$(7.99 \pm 1.28) \cdot 10^{-7}$
B <sub>KCO</sub> (J mol <sup>-1</sup> )	58100 ± 600
A <sub>KCO2</sub> (bar)	$(1.02 \pm 0.16) \cdot 10^{-7}$
$B_{KCO2}$ (J mol <sup>-1</sup> )	67400 ± 600
<i>A<sub>KH2O∕\KH2</sub></i> (bar <sup>-0,5</sup> )	(4.13 ± 1.51)·10 <sup>-11</sup>
$B_{KH2O/\sqrt{KH2}}$ (J mol <sup>-1</sup> )	104500 ± 1100

Source: Graaf; Stamhuis; Beenackers, 1988.

Riquelme (2020) adjusted the model of Vanden Bussche and Froment and the model of Graaf, Stamhuis and Beenackers to kinetic data obtained at 20 bar with two sets of temperatures, 240°C and 260°C, over a commercial Cu/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst (CuO 63.5%, ZnO 24.7%, Al<sub>2</sub>O<sub>3</sub> 10%, and MgO 1.3%) and a Cu/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst synthesized in the laboratory (CuO 60%, ZnO 30%, and Al<sub>2</sub>O<sub>3</sub> 10%). The parameters found by the author are in Tables 4 and 5.

Table 4 – Kinetic parameters obtained by Riquelme (2020) with the kinetic model of Vanden Bussche and Froment (1996)

Parameter	Value estimated for	Value estimated for
	synthesized catalyst	commercial catalyst
$A_{\sqrt{KH2}}$ (bar <sup>-0,5</sup> )	0.644	0.376
$B_{\sqrt{KH2}}$ (J mol <sup>-1</sup> )	21719	23183
A <sub>KH2O</sub> (bar <sup>-1</sup> )	3.31·10 <sup>-7</sup>	3.31·10 <sup>-7</sup>
$B_{KH2O}$ (J mol <sup>-1</sup> )	96829	88741
A <sub>KH2O/K15*K16*KH2</sub>	1064.90	2716.61
A <sub>k1</sub> (mol kg <sup>-1</sup> s <sup>-1</sup> bar <sup>-1</sup> )	5.90·10 <sup>9</sup>	1.88·10 <sup>10</sup>
$B_{k1}$ (J mol <sup>-1</sup> )	-48144	-70605

Source: Riquelme, 2020.

Table 5 – Kinetic parameters obtained by Riquelme (2020) with the kinetic model of Graaf, Stamhuis and Beenackers (1988)

D 1	Value estimated for	Value estimated for
Parameter	synthesized catalyst	commercial catalyst
A <sub>k1</sub> (mol s <sup>-1</sup> kg <sup>-1</sup> bar <sup>-0.5</sup> )	1.96·10 <sup>9</sup>	2.26·10 <sup>10</sup>
$B_{k1}$ (J mol <sup>-1</sup> )	-189348	-292083
A <sub>KCO</sub> (bar)	4.87·10 <sup>-2</sup>	7.62·10 <sup>-2</sup>
$B_{KCO}$ (J mol <sup>-1</sup> )	86017	64162
A <sub>KCO2</sub> (bar)	1.04·10 <sup>-2</sup>	1.01·10 <sup>-2</sup>
$B_{KCO2}$ (J mol <sup>-1</sup> )	31623	33224
<i>A<sub>KH2O</sub>√<sub>KH2</sub></i> (bar <sup>-0,5</sup> )	2.90·10 <sup>-5</sup>	2.21·10 <sup>-6</sup>
$B_{KH2O \wedge KH2}$ (J mol <sup>-1</sup> )	9.32	67795

Source: Riquelme, 2020.

Dehghanpoor *et al.* (2022), in their feasibility study of the conversion of petrochemical off-gas streams to methanol over a commercial CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst, evaluated parameters for the model of Graaf, Stamhuis, and Beenackers (1988) using real plant data. They reported the parameters presented in Table 6.

Table 6 – Kinetic parameters obtained by Dehghanpoor *et al.* (2022) with the kinetic model of Graaf, Stamhuis and Beenackers (1988)

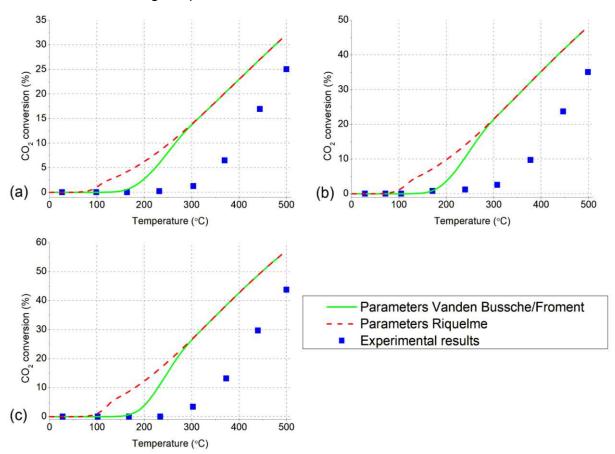
Parameter	Value
A <sub>k1</sub> (mol s <sup>-1</sup> kg <sup>-1</sup> bar <sup>-0.5</sup> )	9.64·10 <sup>11</sup>
$B_{k1}$ (J mol <sup>-1</sup> )	-152900.00
A <sub>KCO</sub> (bar)	2.14·10 <sup>-5</sup>
B <sub>KCO</sub> (J mol⁻¹)	47120.51
A <sub>KCO2</sub> (bar)	$7.92 \cdot 10^{-7}$
$B_{KCO2}$ (J mol <sup>-1</sup> )	62148.78
<i>A<sub>κH2O</sub>/</i> <sub>κH2</sub> (bar <sup>-0,5</sup> )	4.39·10 <sup>-9</sup>
$B_{KH2O \wedge KH2}$ (J mol <sup>-1</sup> )	84350.46

Source: Dehghanpoor et al., 2022.

The model of Vanden Bussche and Froment (1996) was employed for the simulation of the light-off curves using the values of the kinetic parameters reported

in the original paper and using the parameters estimated by Riquelme (2020). The model of Graaf, Stamhuis, and Beenackers (1988) was employed using the original parameters and the parameters proposed by the works of Riquelme (2020) and Dehghanpoor *et al.* (2022). The results of these simulations are presented in Figures 11 and 12, compared with the experimental data.

Figure 11 – Comparison between the experimental light-off curves at 30 m³ kg⁻¹ h⁻¹ and the simulation through the Vanden Bussche and Froment model with original parameters

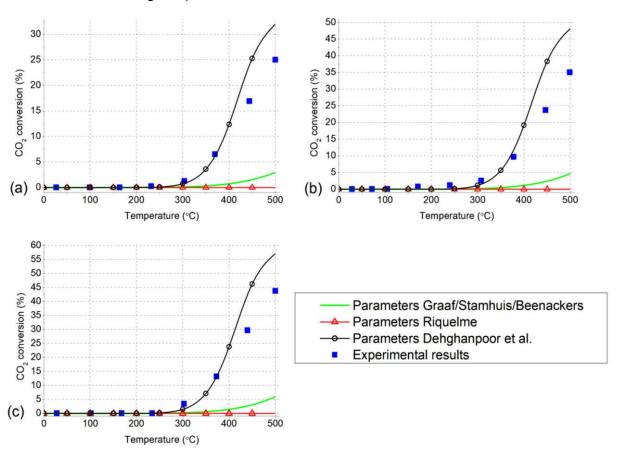


Legend: (a)  $-H_2/CO_2$  molar ratio of 1:1; (b)  $-H_2/CO_2$  molar ratio of 2.5:1; (c)  $-H_2/CO_2$  molar ratio of 4:1. Source: The author, 2024.

Figure 11 shows that the introduction of the original Vanden Bussche and Froment parameters into the reactor model for the conditions used in the light-off tests was not able to reproduce the behavior observed in the catalytic tests faithfully, predicting conversions higher than the experimental conversions from 160 °C onwards for all compositions analyzed. The parameters provided by Riquelme (2020) led to a result very similar to that observed with the Vanden Bussche and Froment

parameters, except in the range between 100 °C and 300 °C, where the Riquelme (2020) parameters produce higher conversions than the original parameters.

Figure 12 – Comparison between the experimental light-off curves at 30 m³ kg⁻¹ h⁻¹ and the simulation through the Graaf, Stamhuis, and Beenackers model with original parameters



Legend: (a)  $-H_2/CO_2$  molar ratio of 1:1; (b)  $-H_2/CO_2$  molar ratio of 2.5:1; (c)  $-H_2/CO_2$  molar ratio of 4:1. Source: The author, 2024.

Figure 12 shows that the original parameters of Graaf, Stamhuis, and Beenackers provide significantly lower conversions than those obtained experimentally. The simulation using the parameters reported by Riquelme (2020) underestimates even more significantly the CO<sub>2</sub> conversion. While these two sets of parameters predict a very late onset of CO<sub>2</sub> conversion along the temperature ramp, the parameters of Dehghanpoor (2022), in turn, manage to reasonably reproduce the trend of the experimental data up to approximately 370 °C, when the calculated conversion starts to be quite above the experimental values.

The large difference in the fit of the reactor model to the experimental data using the parameters from the literature reflects the difficulty of extrapolating the use of kinetic parameters to different experimental conditions. In the studies by Vanden Bussche and Froment (1996), Riquelme (2020), and Graaf, Stamhuis, and Beenackers (1988), experiments were carried out at pressures between 15 and 51 bar and in a temperature range from 180 °C to 280 °C. The specific experimental conditions used by Dehghanpoor *et al.* (2022) in adjusting the parameters were not explained. This temperature window is narrow compared to the range covered by the light-off tests, which may help to explain the wide deviation from the experimental conversions when these parameters are used to model the reactor. Other possible causes for the discrepancy observed between the experimentally observed behavior and the predictions obtained with kinetic parameters from the literature involve possible differences in formulation and/or preparation technique of the catalysts and the significant distance between the pressure levels applied in the kinetic studies analyzed and the atmospheric pressure used in the present work.

#### 3.8 Kinetic parameter estimation

The reactor model with the reaction rate proposed by Ginés, Marchi, and Apesteguía (1997) was fitted to the light-off experimental data obtained in this work. Table 7 lists the values obtained for the proposed parameters.

Table 7 - Parameters estimated using the kinetic model of Ginés, Marchi, and Apesteguía (1997)

Parameter	Value	
k <sub>1,0</sub> ⋅L <sub>0</sub> (mol h <sup>-1</sup> g <sup>-1</sup> atm <sup>-1</sup> )	1.034·10 <sup>9</sup>	
E <sub>a,1</sub> (kcal mol⁻¹)	22.82	
k <sub>4,0</sub> (atm <sup>-1</sup> )	5.131	
$\Delta E_{a,4}$ (kcal mol <sup>-1</sup> )	2.014	
<i>k<sub>5,0</sub></i> (atm⁻¹)	6.963·10 <sup>-5</sup>	
$\Delta E_{a,5}$ (kcal mol <sup>-1</sup> )	0.0491	

The same procedure was adopted for the models of Vanden Bussche and Froment (1996) and Graaf, Stamhuis, and Beenackers (1988), providing the estimation of the parameters shown in Tables 8 and 9.

Table 8 – Parameters estimated using the kinetic model of Vanden Bussche and Froment (1996)

Parameter	Value
A <sub>√KH2</sub> (bar <sup>-0,5</sup> )	0.300
$B_{\sqrt{KH2}}$ (J mol <sup>-1</sup> )	10030.7
A <sub>KH2O</sub> (bar <sup>-1</sup> )	1.00·10 <sup>-11</sup>
$B_{KH2O}$ (J mol <sup>-1</sup> )	91163.8
A <sub>KH2O/K15*K16*KH2</sub>	3991.59
A <sub>k1</sub> (mol kg s <sup>-1</sup> bar <sup>-1</sup> )	1.00·10 <sup>9</sup>
$B_{k1}$ (J mol <sup>-1</sup> )	-111053.8

Source: The author, 2024.

Table 9 – Parameters estimated using the kinetic model of Graaf, Stamhuis, and Beenackers (1988)

Parameter	Value
A <sub>k1</sub> (mol s <sup>-1</sup> kg <sup>-1</sup> bar <sup>-0.5</sup> )	3.16·10 <sup>8</sup>
$B_{k1}$ (J mol <sup>-1</sup> )	-92897.6
A <sub>KCO</sub> (bar)	2.29·10 <sup>-6</sup>
B <sub>KCO</sub> (J mol <sup>-1</sup> )	89986.3
A <sub>KCO2</sub> (bar)	2.21·10 <sup>-7</sup>
$B_{KCO2}$ (J mol <sup>-1</sup> )	53564.6
<i>A<sub>KH2O∕\KH2</sub></i> (bar <sup>-0,5</sup> )	9.71·10 <sup>-9</sup>
$B_{KH2ONKH2}$ (J mol <sup>-1</sup> )	109957.8

Source: The author, 2024.

Performing catalytic runs in an integral reactor at 1 atm in the 493–523 °C temperature range, with a 2–40 g h mol<sup>-1</sup> contact time range and a  $H_2/CO_2$  molar ratio of 6 in the feed, Ginés, Marchi, and Apesteguía (1997) obtained kinetic data to fit the parameters of their kinetic model, presented in Table 10. They plotted the  $ln(k_1L_0)$  values as a function of the inverse of the temperature to calculate the

apparent activation energy of the RWGS reaction, presented in Table 11, together with other values available in the literature and the value of  $E_{a,1}$  found in the present work through the kinetic model of Ginés, Marchi, and Apesteguía (1997). It can be observed that the estimated value is within the range of reported values.

Table 10 – Kinetic parameters obtained by Ginés, Marchi, and Apesteguía (1997) in their kinetic model, according to the temperature

Temperature (K)	k <sub>1</sub> L <sub>0</sub> (mol h <sup>-1</sup> g <sup>-1</sup> atm <sup>-1</sup> )	K <sub>8</sub> * (atm <sup>-1</sup> )
493	0.0200 ± 0.0015	0.060 ± 0.008
503	$0.0487 \pm 0.0044$	0.051 ± 0.004
513	0.0711 ± 0.0070	0.041 ± 0.007
523	0.1287 ± 0.0077	$0.039 \pm 0.002$

Source: Ginés; Marchi; Apesteguía, 1997.

Table 11 – Apparent activation energy values reported in the literature

Reference	Apparent activation	Catalyst
	energy (kJ mol <sup>-1</sup> )	<b>-,</b>
Ginés, Marchi and Apesteguía (1997)	100.4	CuO/ZnO/Al <sub>2</sub> O <sub>3</sub>
Van Herwijnen and de Jong (1980)	98.3	Cu/ZnO
Ernst, Campbell and Moretti (1992)	75.3	Cu(110)
Yoshihara and Campbell (1996)	78.0	Cu(110)
Purnama <i>et al</i> . (2004)	108.0	CuO/ZnO/Al <sub>2</sub> O <sub>3</sub>
Jadhav and Vaidya (2020)	72.4	CuO/ZnO/Al <sub>2</sub> O <sub>3</sub>
This work (2024)	95.5	$CuO/ZnO/Al_2O_3$

Source: The author, 2024.

The average relative error for each kinetic model was calculated using equation (109):

$$Average \ relative \ error = \frac{\sum \left(\frac{|X_{CALC} - X_{EXP}|}{X_{EXP}}\right) \cdot 100\%}{Number \ of \ catalytic \ runs} \tag{109}$$

The average relative error and the minimum value of the objective function found after optimization are presented in Table 12.

Table 12 – Average relative error and values of  $f_{obj}$  after the estimation of the parameters for each kinetic model studied

Model	Average relative error (%)	f <sub>obj</sub>
Ginés, Marchi and Apesteguía (1997)	16.9	0.0020
Vanden Bussche and Froment (1996)	11.6	0.0039
Graaf, Stamhuis and Beenackers (1988)	12.3	0.0011

Source: The author, 2024.

The results listed in Table 12 indicate a virtually equivalent quality of fit for the three models, with a slight emphasis on the models by Vanden Bussche and Froment (1996) and Graaf, Stamhuis, and Beenackers (1988), which provided the lowest average error and the lowest value for the objective function, respectively.

Regarding the reaction scheme, the three models have in common the fact that they are based on the adsorption of  $CO_2$  and the dissociative adsorption of  $H_2$ .

The models by Vanden Bussche and Froment (1996) and Ginés, Marchi, and Apesteguía (1997) present the greatest degree of similarity between them. Both assume a redox mechanism that occurs only on the copper surface, with zinc oxide playing merely a structural promotion role. In this mechanism, metallic copper is the active site consecutively oxidized and reduced by CO<sub>2</sub> and H<sub>2</sub>. Furthermore, in both studies, the dissociative adsorption of CO<sub>2</sub> (23) is indicated as the rate-determining step.

$$CO_{2(g)} + S \rightleftharpoons CO_{(g)} + O_{(a)}$$
 (23)

The two models differ concerning water formation and desorption. The reaction route proposed by Ginés, Marchi, and Apesteguía (1997) describes the formation of water in a direct manner, with two individually adsorbed hydrogen atoms combining with an adsorbed oxygen atom to form water, according to the reaction (24):

$$2H_{(a)} + O_{(a)} \rightleftharpoons H_2O_{(g)} \tag{24}$$

The reaction route of Ginés, Marchi, and Apesteguía (1997) does not take into account intermediate stages of desorption, neither of water nor of carbon monoxide, because the authors assumed a low coverage of these adsorbates under the temperature and partial pressure conditions used in the work. The mechanism related to the Vanden Bussche and Froment (1996) model also does not involve a CO desorption step but considers the water desorption step, which they describe as relatively slow. Furthermore, the formation of water is assumed to occur in two stages. In the first (15), an adsorbed O atom is hydrogenated, giving rise to an intermediate hydroxyl species; in the second (16), the hydroxyl interacts with a second adsorbed H atom to form water, which is subsequently desorbed in stage (17).

$$H_{(a)} + O_{(a)} \rightleftharpoons OH_{(a)} + S$$
 (15)

$$H_{(a)} + OH_{(a)} \rightleftharpoons H_2O_{(a)} + S$$
 (16)

$$H_2O_{(a)} \rightleftharpoons H_2O_{(g)} + S$$
 (17)

The lower average error obtained with the Vanden Bussche and Froment model indicates that taking into account the intermediate stages of water formation and desorption may have contributed to greater accuracy. Even so, the difference between the errors was relatively small, and it is possible to consider that the assumptions made in the Ginés, Marchi, and Apesteguía model meet a compromise between a simplified mechanism and a faithful representation of the system behavior, even achieving a lower value for  $f_{obj}$  with this model.

On the other hand, Graaf, Stamhuis, and Beenackers (1988) assumed a dualsite associative mechanism via formate route, in which CO and  $CO_2$  adsorb competitively on site 1, and  $H_2$  and  $H_2O$  adsorb competitively on site 2.

$$CO_{2(g)} + S_1 \rightleftharpoons CO_{2(a)} \tag{33}$$

$$H_{2(g)} + 2S_2 \rightleftharpoons 2H_{(a)}$$
 (34)

$$CO_{2(a)} + H_{(a)} \rightleftharpoons HCO_{2(a)} + S_2$$
 (35)

This reaction route considers the ability of ZnO to activate the  $H_2$  molecule through its dissociative adsorption while it is not capable of adsorbing carbon monoxide, as opposed to  $Cu^+$ , which can adsorb CO and not  $H_2$ . Therefore, the type

2 sites responsible for the scission of the H<sub>2</sub> molecule may be associated with ZnO, while the type 1 sites would be related to Cu<sup>+</sup> and its adjacent oxygen vacancies, capable of promoting the adsorption of CO and CO<sub>2</sub>. After a statistical evaluation, Graaf, Stamhuis, and Beenackers pointed out the hydrogenation of the formate intermediate as the rate-determining step, which produces CO adsorbed at site 1 and water adsorbed at site 2 (Graaf; Stamhuis; Beenackers, 1988; Herman *et al.*, 1979; Riquelme, 2020).

$$HCO_{2(a)} + H_{(a)} \rightleftharpoons CO_{(a)} + H_2O_{(a)}$$
 (36)

In addition to the form of water generation, the mechanism differs from that observed in the other two models by considering the desorption of both water and carbon monoxide (Graaf; Stamhuis; Beenackers, 1988).

$$CO_{(a)} \rightleftharpoons CO_{(g)} + S_1 \tag{37}$$

$$H_2O_{(a)} \rightleftharpoons H_2O_{(g)} + S_2$$
 (38)

The minimum value of the objective function achieved with the Graaf, Stamhuis, and Beenackers (1988) model was lower than with the other two models, indicating that the assumed reaction path may have led to lower absolute errors. However, the average relative error is still higher than that provided by the Vanden Bussche and Froment (1996) model, indicating a slightly greater precision with the redox mechanism.

#### 3.9 Light-off curves simulation using parameter estimation results

The parameters obtained from adjusting the experimental data were introduced into the reactor model to simulate the light-off curves. The following graphs compare the calculated curves from 25 °C to 500 °C with the three models studied and the experimental results under the same operational conditions. Figures 13, 14, and 15 are associated with  $H_2/CO_2$  molar ratios of 1:1, 2.5:1, and 4:1

respectively. In all scenarios, the space velocity was the same as that used in the light-off experiments, 30 m³ kg⁻¹ h⁻¹. The graphs reveal a satisfactory agreement between the model predictions and the experimental data. The shape of the experimental curve was represented reasonably well for the three models analyzed, but the joint plotting allows us to observe a better fitting with the model by Vanden Bussche and Froment, which for almost all points is slightly closer to the experimental points than the other two rate equations, highlighting the smaller relative error obtained with the Vanden Bussche and Froment model. Both the effect of temperature variation and the effect of feed composition variation were successfully predicted by the investigated models with the estimated parameters, and it was possible to observe the sharp increase in CO₂ conversion along the temperature ramp and the higher conversion achieved for higher H₂/CO₂ ratios.

Figure 13 – Comparison between the simulated light-off curves and the experimental data with H<sub>2</sub>/CO<sub>2</sub> molar ratio of 1:1

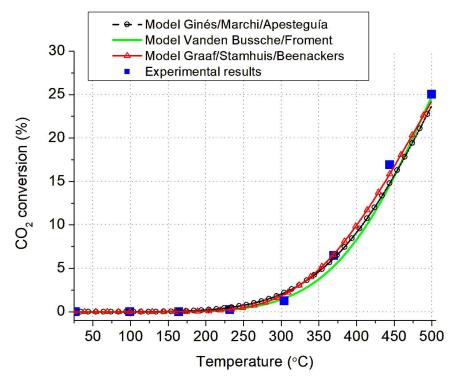


Figure 14 – Comparison between the simulated light-off curves and the experimental data with H<sub>2</sub>/CO<sub>2</sub> molar ratio of 2.5:1

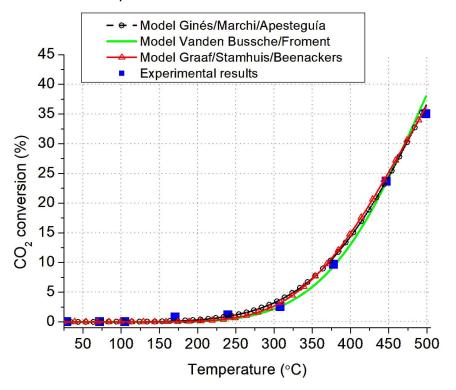


Figure 15 – Comparison between the simulated light-off curves and the experimental data with H<sub>2</sub>/CO<sub>2</sub> molar ratio of 4:1

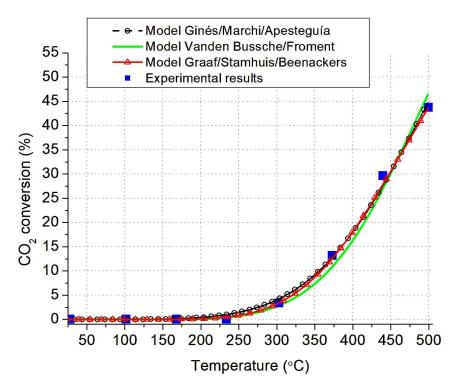


Figure 16 presents a parity plot for the carbon dioxide conversion with the three models studied. The proximity of the points to the diagonal line shows the agreement between the measured conversion values, present in the experimental light-off curves, and the model estimates for the corresponding conditions. Furthermore, the absence of trends in the deviations from the bisector indicates that these are random deviations. Table 13 lists the values of the coefficient of determination (R2) obtained for each model. In all three cases, the value of R2 is reasonably close to 1, confirming that the three models provided a satisfactory fit to the experimental data. The parity plot with the model by Graaf, Stamhuis, and Beenackers (1988) had the highest coefficient of determination.

50 50 Calculated CO, conversion (%) Calculated CO, conversion (%) 20 20 10 10 40 50 50 (a) (b) Experimental CO, conversion (%) Experimental CO, conversion (%) 50 Calculated CO, conversion (%) Ginés, Marchi and Apesteguía (1997) 30 Vanden Bussche and Froment (1996) Graaf, Stamhuis and Beenackers (1988) x = y40 50 (c) Experimental CO, conversion (%)

Figure 16 – Parity plots for CO<sub>2</sub> conversion in light-off curves

Legend: (a) - Model of Ginés, Marchi and Apesteguía (1997); (b) - Model of Vanden Bussche and Froment (1996); (c) - Model of Graaf, Stamhuis and Beenackers (1988).

Table 13 – Coefficient of determination (R<sup>2</sup>) of parity plots related to kinetic models

Model	R²	
Ginés, Marchi and Apesteguía (1997)	0.9951	
Vanden Bussche and Froment (1996)	0.9917	
Graaf, Stamhuis and Beenackers (1988)	0.9971	

# 3.10 Comparison between parameters from light-off curves data and parameters obtained with steady-state data

The kinetic models studied were applied in a new parameter estimation, now using data from tests at fixed temperatures. For the three models, the results obtained with the data at temperature levels were considerably similar to the results obtained using the light-off curves. However, the model by Vanden Bussche and Froment (1996) stands out due to the similarity of the numerical values of the parameters adjusted in both approaches. Therefore, the results obtained with the model by Vanden Bussche and Froment were selected to be presented in Table 14, which compares the set of parameters adjusted with the data from the light-off curves and the new parameters estimated through the more conventional procedure with data obtained in steady-state, while Table 15 compares the mean relative error and the minimum value for the objective function in the two approaches.

Table 14 – Comparison between the parameters estimated using the model of

Vanden Bussche and Froment (1996) with data from tests at temperature

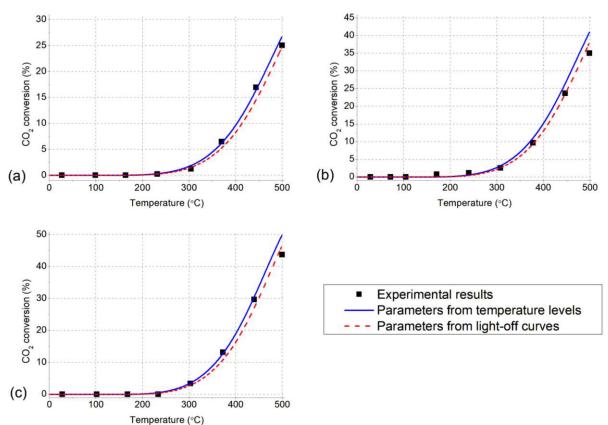
levels and data from light-off curves

Parameter	Temperature levels	Light-off curves
A <sub>√KH2</sub> (bar <sup>-0,5</sup> )	0.250	0.300
$B_{\sqrt{KH2}}$ (J mol <sup>-1</sup> )	10072.1	10030.7
A <sub>KH2O</sub> (bar <sup>-1</sup> )	5.00·10 <sup>-12</sup>	1.00·10 <sup>-11</sup>
$B_{KH2O}$ (J mol <sup>-1</sup> )	90053.5	91163.8
A <sub>KH2O/K15*K16*KH2</sub>	3958.48	3991.59
<i>A<sub>k1</sub></i> (mol kg s <sup>-1</sup> bar <sup>-1</sup> )	1.00·10 <sup>9</sup>	1.00·10 <sup>9</sup>
$B_{k1}$ (J mol <sup>-1</sup> )	-109227.3	-111053.8

Table 15 – Comparison of average relative error and  $f_{obj}$  for parameters estimated using the model by Vanden Bussche and Froment (1996) with data from tests at temperature levels and data from light-off curves

Approach	Average relative error (%)	$f_{obj}$	
Temperature levels	14.8	0.0064	
Light-off curves	11.6	0.0039	

Figure 17 – Comparison between the simulated light-off curves by the model of Vanden Bussche and Froment (1996) using parameters obtained with fixed-temperature tests and experimental light-off curves



Legend: (a)  $-H_2/CO_2$  molar ratio of 1:1; (b)  $-H_2/CO_2$  molar ratio of 2.5:1; (c)  $-H_2/CO_2$  molar ratio of 4:1.

The new parameters fitted through the steady-state experimental data were used to simulate the light-off curves at 30 m<sup>3</sup> kg<sup>-1</sup> h<sup>-1</sup> for the three mixtures. Figure 17 presents a comparison between the predictions obtained with the two approaches.

The simulated light-off curves show that the parameters fitted with temperature ramp data are slightly closer to most experimental points, a trend confirmed by the lower values of mean error and  $f_{obj}$  found in this approach. Although the fit with the parameters provided by steady-state data was satisfactory, Figure 17 shows that the deviations increase above 430 °C, when the simulation extrapolates the range covered by the tests at temperature levels. The similarity between the estimates in the two approaches also suggests that the heating rate applied in tests at the temperature ramp (5 °C min<sup>-1</sup>) provided sufficient time to reach a steady state. That is

one of the main conditions required for the use of data from transient tests in the modeling of catalytic reactions. Catalyst deactivation, diffusion limitations, and an excessively high heating rate can affect the prediction provided by temperature ramp data (Duprat, 2002; Mello, 2017).

In addition to light-off curves providing parameters capable of describing the system behavior over a broader temperature range, this approach involves considerably less experimental effort. Obtaining the steady-state kinetic data required 27 experiments, while the experimental light-off curves needed three tests. These results indicate that modeling the kinetics of the RWGS reaction from data extracted from light-off curves is a viable and advantageous possibility in terms of accuracy and use of time, energy, and resources. It is noteworthy that, at the time of carrying out this work, no research was found in the literature evaluating the feasibility of extracting kinetic data from experimental light-off curves for the RWGS reaction.

#### CONCLUSIONS

The present work studied the conversion of carbon dioxide to carbon monoxide through the reverse gas-water shift (RWGS) reaction as an alternative to reduce the concentration of greenhouse gases in the atmosphere. Catalytic tests were performed over a commercial CuO/ZnO/Al<sub>2</sub>O<sub>3</sub> catalyst to obtain CO<sub>2</sub> conversion data in temperature ramp experiments (light-off curves) and at fixed temperatures. One of the goals is to determine new values of the kinetic parameters of three rate models available in the literature and identify which model attains the best adherence to the experimental data.

The results of the experiments at fixed temperatures indicated, as expected, that CO<sub>2</sub> conversion is favored under conditions of higher temperature, lower space velocity, and higher molar ratio H<sub>2</sub>/CO<sub>2</sub>. It was also observed that the experimental values of conversion in temperature ramp were consistent with the steady-state tests, allowing the kinetic parameters to be estimated from the light-off tests. This approach allows obtaining larger sets of data for kinetic studies with a smaller number of experiments required and less time consumption.

The parameters were fitted to the experimental data using the reaction rate expressions proposed by Ginés, Marchi and Apesteguía (1997), Vanden Bussche and Froment (1996) and Graaf, Stamhuis and Beenackers (1988), with an average error of 16.9%, 11.6% and 12.3%, respectively. These results indicate that the model presented by Vanden Bussche and Froment (1996) is associated with the smallest average error.

The comparison between the reactor simulation and the experimental data showed that the estimated parameters provided a good prediction of the CO<sub>2</sub> conversion profile along the temperature ramp, even with the use of a steady-state pseudo-homogeneous reactor model, confirming the validity of the assumed hypotheses and the compatibility of the applied heating rate with the time required to reach steady state.

Simulating the light-off curves with the parameters reported in the literature, it was not possible to faithfully reproduce the experimental data, indicating that extrapolation of the use of kinetic parameters obtained in the steady state outside the range of the experimental conditions employed may compromise the accuracy of the

predictions provided. Extracting kinetic parameters from light-off curves can mitigate this problem, due to the wider temperature range covered by these data.

From the data obtained from the fixed temperature tests, a new set of parameters was fitted using the Vanden Bussche and Froment (1996) model. The parameter values were relatively similar to those obtained from the light-off curves. The simulation of the CO<sub>2</sub> conversion as a function of temperature with both sets of parameters confirmed that the light-off curves were able to lead to a satisfactory prediction of the RWGS reaction over a wider temperature range with less experimental effort.

After all, it was possible to conclude that temperature ramp tests are capable of providing valuable kinetic information to acquire a broader knowledge of the RWGS reaction, enabling an advance in the level of maturity of this technology, which represents a promising alternative towards a decarbonization process.

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#### **APPENDIX A –** Deduction of dimensionless models

## A.1 Model of Ginés, Marchi and Apesteguía (1997)

The reactor model in terms of Ginés, Marchi and Apesteguía rate equation is, in principle, expressed as:

$$\frac{dF_{CO_2}}{dW} = -\frac{k_1 L_0 \left( P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1} \right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_8^* K_{24}^*} \cdot P_{CO}}$$
(110)

$$\frac{dF_{H_2}}{dW} = -\frac{k_1 L_0 \left( P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1} \right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_8^* K_{24}^*} \cdot P_{CO}}$$
(111)

$$\frac{dF_{CO}}{dW} = \frac{k_1 L_0 \left( P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1} \right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_9^* K_{24}^*} \cdot P_{CO}}$$
(112)

$$\frac{dF_{H_2O}}{dW} = \frac{k_1 L_0 \left( P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1} \right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_0^* K_{2A}^*} \cdot P_{CO}}$$
(113)

$$\frac{dF_{He}}{dW} = 0 ag{114}$$

Given hypothesis (f) of ideal gas conditions, the molar flow rates are calculated through ideal gas law:

$$P \cdot V = n \cdot R \cdot T \tag{115}$$

where P is the pressure in atm, V is the volume in L, n is the number of moles in mol, R is the universal gas constant in L atm  $K^{-1}$  mol<sup>-1</sup>, and T is the temperature in K. This equation can also be expressed for flow rates:

$$P \cdot q = F_T \cdot R \cdot T \tag{116}$$

in which q is the volumetric flow rate in L h<sup>-1</sup>, and  $F_T$  is the total molar flow rate in mol h<sup>-1</sup>, that thereby can be calculated by:

$$F_T = \frac{P \cdot q}{R \cdot T} \tag{117}$$

The molar flow rate of species i is determined by equation (118), where  $y_i$  is the molar fraction of species i in the gas phase (dimensionless):

$$F_i = y_i \cdot F_T \tag{118}$$

Therefore, molar flow rates can be expressed in terms of partial pressures:

$$F_i = \frac{P_i \cdot q}{R \cdot T} \tag{119}$$

And the equation (110) becomes:

$$\frac{d\left(\frac{P_{CO_2} \cdot q}{R \cdot T}\right)}{dW} = -\frac{k_1 L_0 \left(P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1}\right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_8^* K_{24}^*} \cdot P_{CO}}$$
(120)

$$\frac{q}{R \cdot T} \cdot \frac{dP_{CO_2}}{dW} = -\frac{k_1 L_0 \left( P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1} \right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_8^* K_{2A}^*} \cdot P_{CO}}$$
(121)

$$\frac{dP_{CO_2}}{dW} = -\frac{\frac{R \cdot T}{q} \cdot k_1 L_0 \left( P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1} \right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_8^* K_{24}^*} \cdot P_{CO}}$$
(122)

Multiplying both sides of equation (122) by  $W_0/P$ :

$$\frac{dP_{CO_2}}{dW} \cdot \frac{W_0}{P} = -\frac{\frac{W_0}{P} \cdot \frac{R \cdot T}{q} \cdot k_1 L_0 \left( P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1} \right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_8^* K_{24}^*} \cdot P_{CO}}$$
(123)

$$\frac{d\left(\frac{P_{CO_2}}{P}\right)}{d\left(\frac{W}{W_0}\right)} = -\frac{\frac{k_1 L_0 \cdot R \cdot T \cdot W_0}{q} \cdot \frac{1}{P} \left(P_{CO_2} P_{H_2} - \frac{P_{CO}^2}{K_1}\right)}{P_{H_2} + \sqrt{K_8^*} \cdot P_{H_2}^{1.5} + \frac{1}{K_8^* K_{24}^*} \cdot P_{CO}} \tag{124}$$

Applying equations (83), (84), (85) and (87):

$$\frac{dy_{CO_2}}{dm} = -\frac{A \cdot \left(\frac{P_{CO_2}}{P} \cdot P_{H_2} - \frac{P_{CO}}{P} \cdot \frac{P_{CO}}{K_1}\right)}{P_{H_2} + \sqrt{K_8^* \cdot y_{H_2}^{1.5} \cdot P^{1.5} + D \cdot P_{CO}}}$$
(125)

Multiplying the right side of the equation (125) by  $\frac{\frac{1}{p}}{\frac{1}{p}}$ :

$$\frac{dy_{CO_2}}{dm} = -\frac{A \cdot \frac{1}{P} \left( y_{CO_2} \cdot P_{H_2} - y_{CO} \cdot \frac{P_{CO}}{K_1} \right)}{\frac{P_{H_2}}{P} + \sqrt{K_8^*} \cdot y_{H_2}^{1.5} \cdot \frac{P^{1.5}}{P} + D \cdot \frac{P_{CO}}{P}}$$
(126)

$$\frac{dy_{CO_2}}{dm} = -\frac{A \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{CO}^2}{K_1}\right)}{y_{H_2} + \sqrt{K_8^*} \cdot y_{H_2}^{1.5} \cdot \sqrt{P} + D \cdot y_{CO}}$$
(127)

Applying equation (86):

$$\frac{dy_{CO_2}}{dm} = -\frac{A \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{CO}^2}{K_1}\right)}{y_{H_2} + B \cdot y_{H_2}^{1.5} + D \cdot y_{CO}}$$
(128)

Performing a similar procedure for equations (111) to (114), the dimensionless model is obtained:

$$\frac{dy_{CO_2}}{dm} = -\frac{A \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{CO}^2}{K_1}\right)}{y_{H_2} + B \cdot y_{H_2}^{1.5} + D \cdot y_{CO}}$$
(68)

$$\frac{dy_{H_2}}{dm} = -\frac{A \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{CO}^2}{K_1}\right)}{y_{H_2} + B \cdot y_{H_2}^{1.5} + D \cdot y_{CO}}$$
(69)

$$\frac{dy_{CO}}{dm} = \frac{A \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{CO}^2}{K_1}\right)}{y_{H_2} + B \cdot y_{H_2}^{1.5} + D \cdot y_{CO}}$$
(70)

$$\frac{dy_{H_2O}}{dm} = \frac{A \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{CO}^2}{K_1}\right)}{y_{H_2} + B \cdot y_{H_2}^{1.5} + D \cdot y_{CO}}$$
(71)

$$\frac{dy_{He}}{dm} = 0 ag{72}$$

## A.2 Model of Vanden Bussche and Froment (1996)

Applying an initial procedure analogous to that carried out for the Ginés, Marchi, and Apesteguía (1997) model, denoted by equations (116) to (119), the Vanden Bussche and Froment (1996) model is expressed in terms of partial pressures:

$$\frac{dP_{CO_2}}{dW} = \frac{-\left(\frac{R \cdot T}{q}\right) \cdot k_1 \cdot P_{CO_2} \cdot \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{P_{H_2O} \cdot P_{CO}}{P_{CO_2} \cdot P_{H_2}}\right)\right)}{\left(1 + \left(\frac{K_{H_2O}}{K_{15}^* K_{16}^* K_{H_2}}\right) \left(\frac{P_{H_2O}}{P_{H_2}}\right) + \sqrt{K_{H_2} \cdot P_{H_2}} + K_{H_2O} \cdot P_{H_2O}\right)} \tag{129}$$

$$\frac{dP_{H_2}}{dW} = \frac{-\left(\frac{R \cdot T}{q}\right) \cdot k_1 \cdot P_{CO_2} \cdot \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{P_{H_2O} \cdot P_{CO}}{P_{CO_2} \cdot P_{H_2}}\right)\right)}{\left(1 + \left(\frac{K_{H_2O}}{K_{15}^* K_{16}^* K_{H_2}}\right) \left(\frac{P_{H_2O}}{P_{H_2}}\right) + \sqrt{K_{H_2} \cdot P_{H_2}} + K_{H_2O} \cdot P_{H_2O}\right)} \tag{130}$$

$$\frac{dP_{CO}}{dW} = \frac{\left(\frac{R \cdot T}{q}\right) \cdot k_1 \cdot P_{CO_2} \cdot \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{P_{H_2O} \cdot P_{CO}}{P_{CO_2} \cdot P_{H_2}}\right)\right)}{\left(1 + \left(\frac{K_{H_2O}}{K_{15}^* K_{16}^* K_{H_2}}\right) \left(\frac{P_{H_2O}}{P_{H_2}}\right) + \sqrt{K_{H_2} \cdot P_{H_2}} + K_{H_2O} \cdot P_{H_2O}\right)} \tag{131}$$

$$\frac{dP_{H_2O}}{dW} = \frac{\left(\frac{R \cdot T}{q}\right) \cdot k_1 \cdot P_{CO_2} \cdot \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{P_{H_2O} \cdot P_{CO}}{P_{CO_2} \cdot P_{H_2}}\right)\right)}{\left(1 + \left(\frac{K_{H_2O}}{K_{15}^* K_{16}^* K_{H_2}}\right) \left(\frac{P_{H_2O}}{P_{H_2}}\right) + \sqrt{K_{H_2} \cdot P_{H_2}} + K_{H_2O} \cdot P_{H_2O}\right)} \tag{132}$$

$$\frac{dP_{He}}{dW} = 0 ag{133}$$

Multiplying equation (129) by  $W_0/P$ :

$$\frac{dP_{CO_2}}{dW} \cdot \frac{W_0}{P} = \frac{-\left(\frac{R \cdot T}{q}\right) \cdot k_1 \cdot P_{CO_2} \cdot \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{P_{H_2O} \cdot P_{CO}}{P_{CO_2} \cdot P_{H_2}}\right)\right) \frac{W_0}{P}}{\left(1 + \left(\frac{K_{H_2O}}{K_{15}^* K_{16}^* K_{H_2}}\right) \left(\frac{P_{H_2O}}{P_{H_2}}\right) + \sqrt{K_{H_2} \cdot P_{H_2}} + K_{H_2O} \cdot P_{H_2O}\right)}$$
(134)

Applying the correction factor  $f_P$  on the right-hand side to transfer the unit of  $k_1$  to mol kg<sup>-1</sup> s<sup>-1</sup> Pa<sup>-1</sup>, and using equation (89):

$$\frac{d\left(\frac{P_{CO_2}}{P}\right)}{d\left(\frac{W}{W_0}\right)} = -\frac{\frac{k_1 \cdot R \cdot T \cdot W_0 \cdot f_P}{q} \cdot \frac{P_{CO_2}}{P} \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{P_{H_2O}P_{CO}}{P_{CO_2}P_{H_2}}\right)\right)}{\left(1 + G\left(\frac{P_{H_2O}}{P_{H_2}}\right) + \sqrt{K_{H_2}P_{H_2}} + K_{H_2O}P_{H_2O}\right)} \tag{135}$$

Applying equations (83), (84), and (88), and multiplying all terms on the right side systematically for P/P:

$$\frac{dy_{CO_2}}{dm} = -\frac{E \cdot y_{CO_2} \left(1 - \left(\frac{1}{K_1}\right) \cdot \left(\frac{P_{H_2O}}{P} \cdot \frac{P}{P_{CO_2}} \cdot \frac{P_{CO}}{P_{H_2}}\right)\right)}{\left(1 + G\left(\frac{P_{H_2O}}{P} \cdot \frac{P}{P_{H_2}}\right) + \sqrt{K_{H_2}P_{H_2}} \cdot \left(\frac{\sqrt{P}}{\sqrt{P}}\right) + K_{H_2O} \cdot P \cdot \frac{P_{H_2O}}{P}\right)} \tag{136}$$

Applying equation (91), and multiplying the right-hand numerator by P/P again:

$$\frac{dy_{CO_2}}{dm} = -\frac{E \cdot y_{CO_2} \left( 1 - \left( \frac{1}{K_1} \right) \cdot \left( \frac{y_{H_2O}}{y_{CO_2}} \cdot \frac{P_{CO}}{P_{H_2}} \cdot \frac{P}{P} \right) \right)}{\left( 1 + G \left( \frac{y_{H_2O}}{y_{H_2}} \right) + \sqrt{K_{H_2}P} \cdot \left( \frac{\sqrt{P_{H_2}}}{\sqrt{P}} \right) + I \cdot \frac{P_{H_2O}}{P} \right)} \tag{137}$$

$$\frac{dy_{CO_2}}{dm} = -\frac{E \cdot y_{CO_2} \left( 1 - \left( \frac{1}{K_1} \right) \cdot \left( \frac{y_{H_2O}}{y_{CO_2}} \cdot \frac{P_{CO}}{P} \cdot \frac{P}{P_{H_2}} \right) \right)}{\left( 1 + G \left( \frac{y_{H_2O}}{y_{H_2}} \right) + \sqrt{K_{H_2}P} \cdot \sqrt{y_{H_2}} + I \cdot y_{H_2O} \right)}$$
(138)

Using equation (90), and applying an analogous procedure to equations (130) to (133), the dimensionless model is obtained:

$$\frac{dy_{CO_2}}{dm} = -\frac{E \cdot y_{CO_2} \left( 1 - \left( \frac{1}{K_1} \right) \cdot \left( \frac{y_{H_2O} \cdot y_{CO}}{y_{CO_2} \cdot y_{H_2}} \right) \right)}{\left( 1 + G \left( \frac{y_{H_2O}}{y_{H_2}} \right) + H \cdot \sqrt{y_{H_2}} + I \cdot y_{H_2O} \right)}$$
(73)

$$\frac{dy_{H_2}}{dm} = -\frac{E \cdot y_{CO_2} \left( 1 - \left( \frac{1}{K_1} \right) \cdot \left( \frac{y_{H_2O} \cdot y_{CO}}{y_{CO_2} \cdot y_{H_2}} \right) \right)}{\left( 1 + G \left( \frac{y_{H_2O}}{y_{H_2}} \right) + H \cdot \sqrt{y_{H_2}} + I \cdot y_{H_2O} \right)}$$
(74)

$$\frac{dy_{CO}}{dm} = \frac{E \cdot y_{CO_2} \left( 1 - \left( \frac{1}{K_1} \right) \cdot \left( \frac{y_{H_2O} \cdot y_{CO}}{y_{CO_2} \cdot y_{H_2}} \right) \right)}{\left( 1 + G \left( \frac{y_{H_2O}}{y_{H_2}} \right) + H \cdot \sqrt{y_{H_2}} + I \cdot y_{H_2O} \right)}$$
(75)

$$\frac{dy_{H_2O}}{dm} = \frac{E \cdot y_{CO_2} \left( 1 - \left( \frac{1}{K_1} \right) \cdot \left( \frac{y_{H_2O} \cdot y_{CO}}{y_{CO_2} \cdot y_{H_2}} \right) \right)}{\left( 1 + G \left( \frac{y_{H_2O}}{y_{H_2}} \right) + H \cdot \sqrt{y_{H_2}} + I \cdot y_{H_2O} \right)}$$
(76)

$$\frac{dy_{He}}{dm} = 0 ag{77}$$

### A.3 Model of Graaf, Stamhuis and Beenackers (1988)

Applying the hypothesis of ideal gas conditions, the fugacity of components is replaced by partial pressure, then the rate equation of Graaf, Stamhuis and Beenackers becomes (Dehghanpoor *et al.*, 2022):

$$r_{RWGS} = \frac{k_1 \cdot K_{CO_2} \cdot \left(P_{CO_2} \cdot P_{H_2} - \frac{P_{H_2O} \cdot P_{CO}}{K_1}\right)}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \left(P_{H_2}^{0.5} + P_{H_2O} \cdot \left(\frac{K_{H_2O}}{K_{H_2}^{0.5}}\right)\right)}$$
(139)

Thus, it is possible to employ the initial procedure described by equations (116) to (119) to obtain the reactor model in terms of partial pressures:

$$\frac{dP_{CO_2}}{dW} = -\left(\frac{R \cdot T}{q}\right) \cdot \frac{k_1 \cdot K_{CO_2} \cdot \left(P_{CO_2} \cdot P_{H_2} - \frac{P_{H_2O} \cdot P_{CO}}{K_1}\right)}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \left(P_{H_2}^{0.5} + P_{H_2O} \cdot \left(\frac{K_{H_2O}}{K_{H_2}^{0.5}}\right)\right)}$$
(140)

$$\frac{dP_{H_2}}{dW} = -\left(\frac{R \cdot T}{q}\right) \cdot \frac{k_1 \cdot K_{CO_2} \cdot \left(P_{CO_2} \cdot P_{H_2} - \frac{P_{H_2O} \cdot P_{CO}}{K_1}\right)}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \left(P_{H_2}^{0.5} + P_{H_2O} \cdot \left(\frac{K_{H_2O}}{K_{H_2}^{0.5}}\right)\right)}$$
(141)

$$\frac{dP_{CO}}{dW} = \left(\frac{R \cdot T}{q}\right) \cdot \frac{k_1 \cdot K_{CO_2} \cdot \left(P_{CO_2} \cdot P_{H_2} - \frac{P_{H_2O} \cdot P_{CO}}{K_1}\right)}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \left(P_{H_2}^{0.5} + P_{H_2O} \cdot \left(\frac{K_{H_2O}}{K_{H_2}^{0.5}}\right)\right)}$$
(142)

$$\frac{dP_{H_2O}}{dW} = \left(\frac{R \cdot T}{q}\right) \cdot \frac{k_1 \cdot K_{CO_2} \cdot \left(P_{CO_2} \cdot P_{H_2} - \frac{P_{H_2O} \cdot P_{CO}}{K_1}\right)}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \left(P_{H_2}^{0.5} + P_{H_2O} \cdot \left(\frac{K_{H_2O}}{K_{H_2}^{0.5}}\right)\right)}$$
(143)

$$\frac{dy_{He}}{dW} = 0 ag{144}$$

Multiplying equation (140) by  $W_0/P$ :

$$\frac{dP_{CO_2}}{dW} \cdot \frac{W_0}{P} = \frac{-\left(\frac{R \cdot T}{q}\right) \cdot k_1 \cdot \frac{W_0}{P} \cdot K_{CO_2} \cdot \left(P_{CO_2} \cdot P_{H_2} - \frac{P_{H_2O} \cdot P_{CO}}{K_1}\right)}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \left(P_{H_2}^{0.5} + P_{H_2O} \cdot \left(\frac{K_{H_2O}}{K_{H_2}^{0.5}}\right)\right)} \tag{145}$$

Applying the correction factor  $f_P$  for pressure on the right-hand side, and using equations (83) and (84):

$$\frac{d\left(\frac{P_{CO_2}}{P}\right)}{d\left(\frac{W}{W_0}\right)} = -\frac{\frac{k_1 \cdot R \cdot T \cdot f_P \cdot W_0}{q \cdot P} \cdot K_{CO_2} \cdot \left(P_{CO_2} \cdot P_{H_2} - \frac{P_{H_2O} \cdot P_{CO}}{K_1}\right)}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \left(P_{H_2}^{0.5} + P_{H_2O} \cdot \left(\frac{K_{H_2O}}{K_{H_2}^{0.5}}\right)\right)} \tag{146}$$

Multiplying the numerator and denominator by  $\frac{\sqrt{P}}{P}$ :

$$\frac{dy_{CO_2}}{dm} = -\frac{\frac{k_1 \cdot R \cdot T \cdot f_P \cdot W_0}{q \cdot P} \cdot K_{CO_2} \cdot \left(P_{CO_2} \cdot P_{H_2} - \frac{P_{H_2O} \cdot P_{CO}}{K_1}\right) \cdot \frac{\sqrt{P}}{P}}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \left(P_{H_2}^{0.5} + P_{H_2O} \cdot \left(\frac{K_{H_2O}}{K_{H_2}^{0.5}}\right)\right) \cdot \frac{\sqrt{P}}{P}} \tag{147}$$

$$\frac{dy_{CO_2}}{dm} = \frac{-\frac{k_1 \cdot R \cdot T \cdot f_P \cdot W_0 \cdot \sqrt{P}}{q \cdot P} \cdot K_{CO_2} \cdot \left(P_{CO_2} \cdot P_{H_2} - \frac{P_{H_2O} \cdot P_{CO}}{K_1}\right) \cdot \frac{1}{P}}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \left(\frac{P_{H_2}^{0.5} \cdot \sqrt{P}}{\sqrt{P} \cdot \sqrt{P}} + \frac{P_{H_2O}}{P} \cdot \left(\frac{K_{H_2O} \cdot \sqrt{P}}{K_{H_2}^{0.5}}\right)\right)} \tag{148}$$

Applying equations (92) and (95):

$$\frac{dy_{CO_2}}{dm} = -\frac{J \cdot K_{CO_2} \cdot \left(\frac{P_{CO_2}}{P} \cdot P_{H_2} - \frac{P_{H_2O}}{P} \cdot \frac{P_{CO}}{K_1}\right)}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(149)

Multiplying the numerator and denominator by *P/P*:

$$\frac{dy_{CO_2}}{dm} = -\frac{J \cdot K_{CO_2} \cdot P \cdot \left(y_{CO_2} \cdot P_{H_2} - y_{H_2O} \cdot \frac{P_{CO}}{K_1}\right) \cdot \frac{1}{P}}{\left(1 + K_{CO} \cdot P_{CO} + K_{CO_2} \cdot P_{CO_2}\right) \cdot \frac{P}{P}\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(150)

Applying equation (94):

$$\frac{dy_{CO_2}}{dm} = -\frac{J \cdot N \cdot \left(y_{CO_2} \cdot \frac{P_{H_2}}{P} - \frac{y_{H_2O} \cdot P_{CO}}{P \cdot K_1}\right)}{\left(\frac{P}{P} + K_{CO} \cdot P \cdot \frac{P_{CO}}{P} + K_{CO_2} \cdot P \cdot \frac{P_{CO_2}}{P}\right) \left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(151)

Using equation (93):

$$\frac{dy_{CO_2}}{dm} = -\frac{J \cdot N \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{H_2O} \cdot y_{CO}}{K_1}\right)}{\left(1 + L \cdot y_{CO} + N \cdot y_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(152)

Applying an analogous procedure to equations (141) to (144) the dimensionless model is obtained:

$$\frac{dy_{CO_2}}{dm} = -\frac{J \cdot N \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{H_2O} \cdot y_{CO}}{K_1}\right)}{\left(1 + L \cdot y_{CO} + N \cdot y_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(78)

$$\frac{dy_{H_2}}{dm} = -\frac{J \cdot N \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{H_2O} \cdot y_{CO}}{K_1}\right)}{\left(1 + L \cdot y_{CO} + N \cdot y_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(79)

$$\frac{dy_{CO}}{dm} = \frac{J \cdot N \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{H_2O} \cdot y_{CO}}{K_1}\right)}{\left(1 + L \cdot y_{CO} + N \cdot y_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(80)

$$\frac{dy_{H_2O}}{dm} = \frac{J \cdot N \cdot \left(y_{CO_2} \cdot y_{H_2} - \frac{y_{H_2O} \cdot y_{CO}}{K_1}\right)}{\left(1 + L \cdot y_{CO} + N \cdot y_{CO_2}\right)\left(\sqrt{y_{H_2}} + y_{H_2O} \cdot Q\right)}$$
(81)

$$\frac{dy_{He}}{dW} = 0 ag{82}$$

## **APPENDIX B –** Equilibrium conversion calculation

Let  $X_{eq}$  be the CO<sub>2</sub> conversion at equilibrium, given by:

$$X_{eq} = \frac{P_{CO_2}^0 - P_{CO_2}^{eq}}{P_{CO_2}^0} \tag{153}$$

in which  $P^0_{CO2}$  is the partial pressure of  $CO_2$  at the inlet in atm, and  $P^{eq}_{CO2}$  is the partial pressure of  $CO_2$  at equilibrium in atm.

Therefore:

$$P_{CO_2}^{eq} = P_{CO_2}^0 \cdot (1 - X_{eq}) \tag{154}$$

While the partial pressures of the other components at equilibrium are given by:

$$P_{H_2}^{eq} = P_{H_2}^0 - P_{CO_2}^0 \cdot X_{eq} \tag{155}$$

$$P_{CO}^{eq} = P_{CO_2}^0 \cdot X_{eq} \tag{156}$$

$$P_{H_2O}^{eq} = P_{CO_2}^0 \cdot X_{eq} \tag{157}$$

being  $P^0_{H2}$  the partial pressure of  $H_2$  at the inlet in atm, and  $P^{eq}_i$  is the partial pressure of component i at equilibrium in atm.

Then the equilibrium constant  $K_1$  is equal to:

$$K_{1} = \frac{P_{CO}^{eq} \cdot P_{H_{2}O}^{eq}}{P_{CO_{2}}^{eq} \cdot P_{H_{2}}^{0}} = \frac{P_{CO_{2}}^{0} \cdot X_{eq} \cdot P_{CO_{2}}^{0} \cdot X_{eq}}{P_{CO_{2}}^{0} \cdot (1 - X_{eq}) \cdot (P_{H_{2}}^{0} - P_{CO_{2}}^{0} \cdot X_{eq})}$$
(158)

However, at a given temperature T, the equilibrium constant for the RWGS reaction can be calculated by equation (28):

$$K_1 = 10^{\left(-\frac{2073}{T} + 2.029\right)} \tag{28}$$

Thus, knowing the temperature and the partial pressures of  $CO_2$  and  $H_2$  at the inlet,  $X_{eq}$  is the value capable of zeroing the value of the objective function  $f^{Xeq}_{obj}$ :

$$f_{obj}^{X_{eq}} = 10^{\left(-\frac{2073}{T} + 2.029\right)} - \frac{P_{CO_2}^0 \cdot X_{eq} \cdot P_{CO_2}^0 \cdot X_{eq}}{P_{CO_2}^0 \cdot \left(1 - X_{eq}\right) \cdot \left(P_{H_2}^0 - P_{CO_2}^0 \cdot X_{eq}\right)}$$
(159)

## **APPENDIX C –** Experimental data from tests at fixed temperatures

Table 16 – Average of experimental CO<sub>2</sub> conversion values in tests at temperature levels with a H<sub>2</sub>/CO<sub>2</sub> molar ratio of 1:1

Temperature (°C)	Space velocity (m³ kg <sup>-1</sup> h <sup>-1</sup> )		
remperature ( 0)	18	30	42
330	3.73	3.05	2.42
380	9.13	7.77	7.43
430	17.1	15.3	14.1

Source: The author, 2024.

Table 17 – Average of experimental  $CO_2$  conversion values in tests at temperature levels with a  $H_2/CO_2$  molar ratio of 2.5:1

Temperature (°C)	Space velocity (m³ kg⁻¹ h⁻¹)		
remperature ( 0)	18	30	42
330	4.42	3.15	2.43
380	13.5	10.8	7.44
430	24.0	19.7	16.4

Source: The author, 2024.

Table 18 – Average of experimental  $CO_2$  conversion values in tests at temperature levels with a  $H_2/CO_2$  molar ratio of 4:1

Temperature (°C)	Space velocity (m³ kg⁻¹ h⁻¹)		
remperature ( o)	18	30	42
330	8.81	7.06	5.65
380	20.0	16.6	13.7
430	32.2	28.9	25.3

## **APPENDIX D –** Experimental data from temperature ramp tests

Table  $19 - \text{Light-off test at } 30 \text{ m}^3 \text{ kg}^{-1} \text{ h}^{-1} \text{ with } \text{H}_2/\text{CO}_2 \text{ molar ratio of } 1:1$ 

Temperature (°C)	CO <sub>2</sub> conversion (%)
27	0.00
99	0.00
164	0.00
232	0.23
304	1.23
370	6.47
444	16.9
500	25.0

Source: The author, 2024.

Table 20 – Light-off test at 30 m³ kg<sup>-1</sup> h<sup>-1</sup> with H<sub>2</sub>/CO<sub>2</sub> molar ratio of 2.5:1

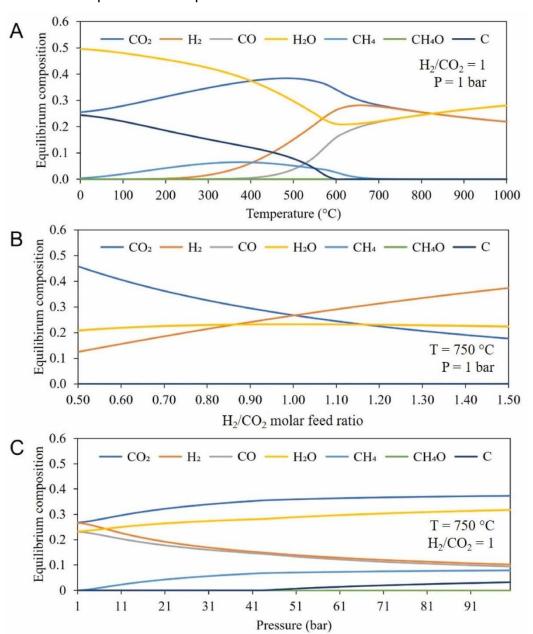
Temperature (°C)	CO <sub>2</sub> conversion (%)
29	0.00
72	0.00
105	0.00
171	0.76
240	1.15
308	2.52
378	9.67
447	23.7
499	35.0

Table 21 – Light-off test at 30  $\mathrm{m^3~kg^{-1}~h^{-1}}$  with  $\mathrm{H_2/CO_2}$  molar ratio of 4:1

Temperature (°C)	CO <sub>2</sub> conversion (%)
28	0.00
102	0.00
168	0.00
234	0.00
303	3.37
373	13.2
440	29.7
500	43.7

#### **ANNEX – Results of simulations from literature**

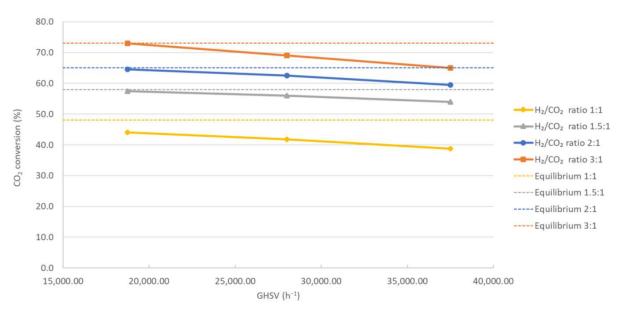
Figure 18 – Evaluation of the effect of different operational parameters on the equilibrium composition



Legend: (a) – Effect of temperature; (b) – Effect of H<sub>2</sub>/CO<sub>2</sub> molar feed ratio; (c) – Effect of pressure.

Source: Santos et al., 2023.

Figure 19 –  $CO_2$  conversion in the RWGS reactor as a function of GHSV at 850 °C



Source: Reinikainen et al., 2022.